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# Numerical turbulence simulations of intermittent fluctuations in the scrape-off layer of magnetized plasmas

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## ABSTRACT

Intermittent fluctuations in the boundary of magnetically confined plasmas are investigated by numerical turbulence simulations of a reduced fluid model describing the evolution of the plasma density and electric drift vorticity in the two-dimensional plane perpendicular to the magnetic field. Two different cases are considered: one describing resistive drift waves in the edge region and another including only the interchange instability due to unfavorable magnetic field curvature in the scrape-off layer. Analysis of long data time series obtained by single-point recordings is compared to predictions of a stochastic model describing the plasma fluctuations as a superposition of uncorrelated pulses. For both cases investigated, the radial particle density profile in the scrape-off layer is exponential with a radially constant scale length. The probability density function for the particle density fluctuations in the far scrape-off layer has an exponential tail. Radial motion of blob-like structures leads to large-amplitude bursts with an exponential distribution of peak amplitudes and the waiting times between them. The average burst shape is well described by a two-sided exponential function. The frequency power spectral density of the particle density is simply that of the average burst shape and is the same for all radial positions in the scrape-off layer. The fluctuation statistics obtained from the numerical simulations are in excellent agreement with recent experimental measurements on magnetically confined plasmas. The statistical framework defines a new validation metric for boundary turbulence simulations.

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#### I. INTRODUCTION

At the boundary of magnetically confined plasma, turbulent transport of particles and heat in the outermost region enhances plasma interactions with the material surfaces. This can become a serious issue for future fusion experiments and reactors.<sup>1–3</sup> A complete description of the physical mechanisms underlying the cross field plasma and heat transport in the scrape-off layer (SOL) and its effects on plasma–wall interactions is necessary if reliable predictions for reactor relevant devices are to be obtained. Unfortunately, such an understanding is at present still not fully achieved and predictions and extrapolations are often based on empirical scaling laws or highly simplified transport modeling with limited theoretical foundation.<sup>3–5</sup>

Fluctuations and turbulent motions in the boundary region of magnetized plasmas have been extensively investigated both experimentally and theoretically. It is recognized that in the SOL, radial motion of blob-like filament structures is the dominant mechanism for cross field transport of particles and heat.<sup>6–9</sup> This leads to broadening and flattening of radial profiles and high average particle density in the SOL that increases plasma-wall interactions.<sup>10–23</sup> Experimental measurements using Langmuir probes and gas puff imaging have revealed highly intermittent fluctuations of the particle density in the far SOL. Interestingly, measurements across a variety of magnetic geometries, including conventional tokamaks, spherical tokamaks, reversed field pinches, and stellarators have shown similar fluctuation characteristics.<sup>24–27</sup> Recent statistical analysis of exceptionally long fluctuation data time series from several tokamak devices has shown that the fluctuations are well described as a superposition of uncorrelated exponential pulses with fixed duration, arriving according to a Poisson process and with exponentially distributed pulse amplitudes.<sup>28–42</sup> A statistical framework based on filtered Poisson processes has proven an accurate description of both average radial profiles and fluctuations in the boundary of magnetically confined plasma.  $^{\rm 43-53}$ 

So far, this stochastic model has not been utilized to analyze fluctuation data from numerical turbulence simulations of the boundary region of magnetized plasmas. In order to obtain statistically significant results, long simulation data time series or a large ensemble is required, equivalent to several hundred milliseconds in experiments with medium-sized magnetically confined plasma. Since most turbulence simulation studies have been focused on the dynamics of individual blob structures or on the effects of specific physical mechanisms on turbulence and transport, the simulations have likely not produced time series data of sufficient duration in order to analyze them in the same manner as the experimental measurements.<sup>28-42</sup> In this paper, we present the first results from applying the same statistical framework on numerical simulation data as has recently been done on experimental measurements. By using a simplified turbulence model describing the fluctuations in the two-dimensional plane perpendicular to the magnetic field, we have obtained data time series sufficiently long to allow unambiguous identification of the fluctuation statistics. The main goal of this study is to clarify these statistical properties and compare them with that found from experimental measurements. This is considered as an essential step toward validation of turbulence simulation codes.5

A recent analysis of fluctuation data time series obtained from numerical simulations of turbulent Rayleigh–Bénard-convection in two dimensions has given some illuminating results.<sup>57</sup> This model has frequently been used as a simplified description of the non-linear interchange dynamics in the SOL of magnetically confined plasmas.<sup>58–66</sup> In Ref. 57, it was found that the fluctuation time series is well described as a superposition of Lorentzian pulses, resulting in an exponential frequency power spectral density. In the present study, more sophisticated models for SOL turbulence are investigated, including sheath dissipation due to losses along magnetic field lines intersecting material surfaces as well as drift wave dynamics in the edge region.<sup>67–83</sup> The resulting far SOL data time series is shown to be dominated by large-amplitude bursts with a two-sided exponential pulse shape and fluctuation statistics that compare favorably with those found in experimental measurements.<sup>28–42</sup>

In this contribution, we present a detailed statistical analysis of fluctuation data time series from numerical simulations of a twodimensional reduced fluid model describing the evolution of the electron density and electric drift vorticity. The paper is structured as follows. The reduced fluid model equations, normalization, and parameters are discussed in Sec. II. A brief introduction to the stochastic model is also presented here. We present the results for the timeaveraged profiles and probability densities in Sec. III and for the fluctuation statistics in Sec. IV. A discussion of the results and the conclusions is finally presented in Sec. V.

#### **II. MODEL EQUATIONS**

The reduced fluid model investigated here is motivated by previous simulation studies performed by Sarazin *et al.*,<sup>69–71</sup> Garcia *et al.*,<sup>72–74</sup> Myra *et al.*,<sup>75–77</sup> Bisai *et al.*,<sup>78–80</sup> and Nielsen *et al.*<sup>81–83</sup> One particular case of the model is equivalent to that used in Ref. 71 and simulates SOL conditions in the entire simulation domain where a particle source is located close to the inner boundary. The particle

density profile results from a balance between the plasma source, the sheath dissipation, and the radial transport due to the interchange instability. Another case of the model is similar to that used in Ref. 79 and features a simulation domain separating an edge region corresponding to plasma dynamics on closed magnetic flux surfaces and a SOL region where sheath dissipation balances the interchange drive. The source term is located in the plasma edge region where parallel resistivity gives rise to unstable drift waves. Despite these two fundamentally different descriptions of the primary instability mechanism underlying the SOL turbulence, the resulting fluctuations are remarkably similar to those will be shown in the following.

Similar to many previous investigations, we use two-field fluid model equations describing the plasma evolution in the edge and SOL regions for a quasi-neutral plasma, neglecting electron inertia and assuming for simplicity isothermal electrons and negligibly small ion temperature.<sup>69–71,78–80</sup> These simplifications lead to a highly efficient numerical implementation of the model equations, allowing us to obtain simulation data time series of unprecedented duration that is suitable for detailed statistical analysis.

We choose a slab geometry where x refers to the radial direction and y to the binormal or poloidal direction. The reduced electron continuity and electron drift vorticity equations are given as

$$\frac{\mathrm{d}n}{\mathrm{d}t} + g\left(\frac{\partial n}{\partial y} - n\frac{\partial \phi}{\partial y}\right) = \Sigma_n + D_\perp \nabla_\perp^2 n + \langle \nabla_\parallel J_{\parallel e} \rangle_\parallel, \quad (1a)$$

$$\frac{\mathrm{d}\nabla_{\perp}^{2}\phi}{\mathrm{d}t} + \frac{g}{n}\frac{\partial n}{\partial y} = \nu_{\perp}\nabla_{\perp}^{4}\phi + \left\langle\frac{1}{n}\nabla_{\parallel}J_{\parallel}\right\rangle_{\parallel},\tag{1b}$$

where *n* represents the normalized electron density,  $\phi$  is the normalized electric potential, g is normalized effective gravity (that is, drive from unfavorable magnetic curvature),  $\Sigma_n$  is the plasma source term, and  $D_{\perp}$  and  $\nu_{\perp}$  are the normalized particle and vorticity diffusion coefficients. We use the standard Bohm normalization as previously used and discussed in Refs. 67-80, that is, spatial units are normalized by the ion sound Larmor radius  $\rho_{s}$ , temporal units by the ion gyration frequency  $\Omega_i = eB/m_i$ , particle density *n* by a characteristic density  $n_0$ , electrostatic potential  $\phi$  by  $T_0/e$ , where  $T_0$  is the electron temperature, parallel electric current,  $J_{\parallel}$  and electron current  $J_{\parallel e}$  by  $en_0c_s$ , where  $c_s$  $= (T_0/m_i)^{1/2}$  is the cold ion sound speed, g is given by  $2\rho_s/R$ , where *R* is the major radius at the low-field side SOL, and  $D_{\perp}$  and  $\nu_{\perp}$  are normalized by  $1/\rho_s^2 \Omega_i$ . In addition, we have the advective derivative  $d/dt = \partial/\partial t + \mathbf{V}_{E} \cdot \nabla_{\perp}$ , where  $\mathbf{V}_{E} = \hat{\mathbf{z}} \times \nabla \phi$  is the electric drift. The plasma source term is given by  $\Sigma_n(x) = \Sigma_0 \exp(-(x-x_0)^2/\lambda_s^2)$ , where  $\Sigma_0$  is the maximum amplitude of the source normalized by  $1/n_0\Omega_i$ ,  $x_0$  is the source location, and  $\lambda_s$  is the *e*-folding length for the source.

Equations (1a) and (1b) are averaged along the magnetic field lines, with the contribution from the normalized parallel electron  $J_{\parallel e}$  and total plasma currents  $J_{\parallel}$  in the sheath connected regime given by

$$\langle \nabla_{\parallel} J_{\parallel e} \rangle_{\parallel} = -\sigma n \exp(\Lambda - \phi) + \chi(\hat{\phi} - \hat{n}),$$
 (2a)

$$\left\langle \frac{1}{n} \nabla_{\parallel} J_{\parallel} \right\rangle_{\parallel} = \sigma [1 - \exp{(\Lambda - \phi)}] + \chi(\hat{\phi} - \hat{n}).$$
 (2b)

Here,  $\Lambda$  is the sheath potential,  $\sigma$  the normalized sheath dissipation coefficient, and  $\chi$  the normalized parallel plasma conductivity. Like in

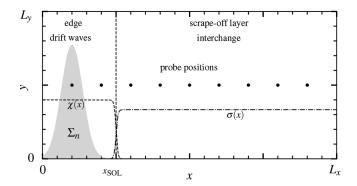
several previous investigations, these parameters are taken to be a function of the radial position in the boundary region.72-83 In particular, the sheath dissipation coefficient  $\sigma$  is finite in the SOL region ( $x > x_{SOL}$ ) and vanishes in the edge ( $x < x_{SOL}$ ), which corresponds to the region with closed magnetic flux surfaces. These two regions are connected with a smooth function due to numerical reasons, that is,  $\sigma(x) = \sigma_0 \{1 + \tanh[w(x - x_{SOL})]\}/2$ . The slope of this function is determined by the width parameter w, which is set to w = 25/32. Similarly, the plasma conductivity  $\chi$  is neglected in the SOL and is finite in the edge region, that is,  $\chi(x)$ =  $\chi_0 (1 - \{1 + \tanh[w(x - x_{\text{SOL}})]\}/2)$ . Here,  $\sigma_0 = \rho_s/L_c$  with  $L_c$  the parallel connection length and  $\chi_0 = (\rho_s k_{\parallel})^2 (m_i/m_e)(\Omega_i/\nu_e)$ , where  $k_{\parallel}$  is the dominant parallel wave number for the edge region drift waves and  $\nu_{ei}$  stands for the collision frequency between electrons and ions. The simulation domain is sketched in Fig. 1, showing the location of the plasma source and the separation between the edge and SOL regions. Furthermore, the spatially fluctuating electron density  $\hat{n}$ and plasma potential  $\phi$  are defined as  $\hat{n} = n - \langle n \rangle_{y}$  and  $\phi = \phi - \langle \phi \rangle_{\nu}$ , where  $\langle \cdot \rangle_{\nu}$  refers to the flux surface average. This leads to the final reduced electron continuity and electric drift vorticity equations,

$$\frac{\mathrm{d}n}{\mathrm{d}t} + g\left(\frac{\partial n}{\partial y} - n\frac{\partial \phi}{\partial y}\right) = \Sigma_n(x) + D_\perp \nabla_\perp^2 n - \sigma(x) n \exp(\Lambda - \phi) + \chi(x)(\hat{\phi} - \hat{n}),$$
(3a)

$$\frac{\mathrm{d}\nabla_{\perp}^{2}\phi}{\mathrm{d}t} + \frac{g}{n}\frac{\partial n}{\partial y} = \nu_{\perp}\nabla_{\perp}^{4}\phi + \sigma(x)[1 - \exp(\Lambda - \phi)] + \chi(x)(\hat{\phi} - \hat{n}).$$
(3b)

In the following, we present results from numerical simulations of this model for two different cases. In the first case, the domain is split into two regions, effectively the edge and the SOL regions, by taking  $x_{\text{SOL}} = 50$ . In the second case, a pure SOL plasma is considered with  $x_{\text{SOL}} = 0$ , and thus, plasma conductivity  $\chi$  is not present in the simulation domain.

The input parameters have been chosen to be similar to that used in previous publications based on this model.<sup>79</sup> For all runs presented here, the simulation domain lengths are chosen to be  $L_x = 200$  and  $L_y$ = 100, with the border between the edge and the SOL at  $x_{SOL} = 50$ 



**FIG. 1.** Schematic illustration of the simulation domain for the  $x_{SOL} = 50$  case. The position of the plasma source term (gray shaded) and the border between edge and SOL (dashed vertical line) are indicated. The radial variation of the sheath dissipation and parallel conductivity coefficients is also shown.

for the two-region case. It has been verified that a change in the size of the simulation domain does not influence the fluctuation statistics. The simulation code is implemented in BOUT++<sup>84</sup> utilizing the STORM branch,<sup>85</sup> which uses a finite difference scheme in the *x*-direction and a spectral scheme in the *y*-direction. Time integration is performed with the PVODE solver.<sup>86</sup> We use a resolution of  $512 \times 256$  grid points for all runs. We further take  $D_{\perp} = \nu_{\perp} = 10^{-2}$ ,  $g = 10^{-3}$ ,  $\chi_0 = 6 \times 10^{-4}$ ,  $\Sigma_0 = 11/2000$ ,  $\sigma_0 = 5 \times 10^{-4}$ , and  $\Lambda = 0.5 \ln(2\pi m_i/m_e)$  with deuterium ions,  $x_0 = 20$  and  $\lambda_s = 10$ . We apply periodic boundary conditions in the poloidal direction and zero gradient boundary conditions at the outer boundary and fixed boundary conditions  $\phi(x = 0) = 0$  at the inner boundary.

During the simulations, the plasma parameters at nine different radial positions in the simulation domain are recorded with a sampling frequency of one in normalized time units. The location of these probes is presented in Fig. 1. This corresponds to single-point measurements in the experiments, and the simulation data will be analyzed in the same manner as has previously been done for experimental measurement data. The contour plots of the electron density in both simulation cases presented in Fig. 2 show several blob-like structures with the familiar mushroom-shape typical for strongly non-linear interchange motions.<sup>65</sup>

Time series of the plasma parameters with a duration of  $2 \times 10^6$  time units has been obtained under statistically stationary conditions, that is, excluding initial transients in the turbulence simulations. Ten simulation runs with this duration time and different random initial conditions are performed for the two-region model and seven for the one region model. The fluctuation statistics to be presented in Sec. IV

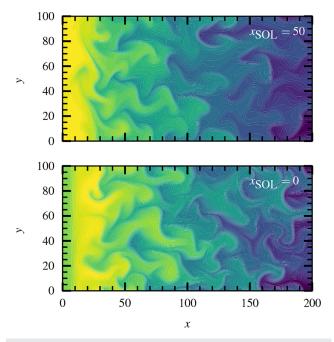


FIG. 2. Contour plots of log(*n*) in the turbulent state for the  $x_{SOL} = 0$  and  $x_{SOL} = 50$  cases showing the presence of mushroom-shaped blob-like structures in the SOL.

are based on these ensembles of simulation data. In the following analysis, we will frequently consider plasma parameters normalized such as to have vanishing mean and unit standard deviation, for example. For the electron density, we define

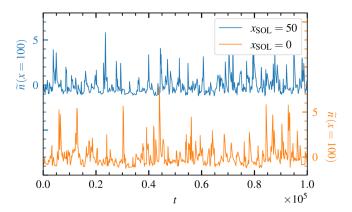
$$\tilde{n} = \frac{n - \langle n \rangle}{n_{\rm rms}},\tag{4}$$

where the angular brackets denote a time average and  $n_{\rm rms}$  is the root mean square value calculated from the time series. A short part of the normalized electron density time series is presented in Fig. 3 for both simulation cases, showing frequent appearance of large-amplitude bursts due to the high density blob-like structures moving radially outwards. The radial variation of the lowest order moments of these fluctuations is presented and discussed in Sec. III. The electron density time series is compared to the radial velocity  $v_x$  and the radial particle flux  $\Gamma = nv_x$  in Fig. 4 for the  $x_{\rm SOL} = 0$  simulation. All quantities are normalized according to Eq. (4). It is shown that large-amplitude events in the particle density are correlated with positive radial velocities resulting in high levels of radial particle transport. The same observations are made for the  $x_{\rm SOL} = 50$  simulation (not presented here).

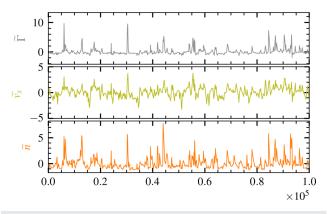
In the following, the numerical simulation data will be compared to predictions of a stochastic model, which describes the fluctuations as a superposition of uncorrelated pulses with fixed shape and constant duration. This is written as<sup>43-55</sup>

$$\Psi_K(t) = \sum_{k=1}^{K(T)} A_k \psi\left(\frac{t - t_k}{\tau_d}\right),\tag{5}$$

where  $\psi$  is the pulse function,  $\tau d$  is the pulse duration time, K(T) is the number of pulses for a realization of duration T, and for the event labeled k the pulse amplitude is  $A_k$  and the arrival time  $t_k$ . The mean value of the random variable  $\Psi_K$  is  $\langle \Psi \rangle = (\tau_d / \tau_w) \langle A \rangle$ , where  $\langle A \rangle$  is the average pulse amplitude and  $\tau w$  is the average pulse waiting time. We will assume pulses arriving according to a Poisson process, which implies independent and exponentially distributed waiting times and independent arrival times uniformly distributed on the realization. We further assume independently and exponentially distributed amplitudes,  $P_A(A) = \exp(-A/\langle A \rangle)/\langle A \rangle$ , and we will consider the case of a two-sided exponential pulse function,<sup>50</sup>



**FIG. 3.** A short part of the normalized electron density time series recorded at x = 100 for the  $x_{SOL} = 0$  and  $x_{SOL} = 50$  simulation cases.



**FIG. 4.** Normalized electron density time series compared to the normalized radial velocity and normalized radial particle flux recorded at x = 100 for the  $x_{SOL} = 0$  simulation case.

$$\psi(\theta;\lambda) = \begin{cases} \exp\left(\frac{\theta}{\lambda}\right), & \theta < 0, \\ \exp\left[-\theta/(1-\lambda)\right], & \theta \ge 0, \end{cases}$$
(6)

where the pulse asymmetry parameter  $\lambda$  is restricted to the range  $0 < \lambda < 1$ . For  $\lambda < 1/2$ , the pulse rise time is faster than the decay time, while the pulse shape is symmetric in the case  $\lambda = 1/2$ . The frequency power spectral density for this process is just the spectrum of the pulse function,<sup>50</sup>

$$\Omega_{\tilde{\Psi}}(\omega) = \frac{2\tau_{\rm d}}{\left[1 + (1 - \lambda)^2 (\tau_{\rm d}\omega)^2\right] \left[1 + \lambda^2 (\tau_{\rm d}\omega)^2\right]},\tag{7}$$

where  $\omega$  is the angular frequency. Note that the power spectral density of  $\tilde{\Psi}$  is independent of the amplitude distribution. From this, it follows that the frequency power spectral density can be used to estimate the pulse parameters  $\tau d$  and  $\lambda$ , which will be done in the following analysis of the numerical simulations.

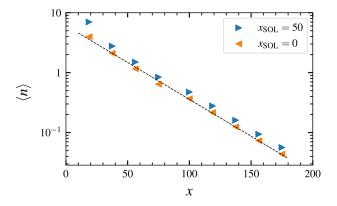
The stationary probability density function (PDF) for the random variable  $\Psi_K$  can be shown to be a gamma distribution,<sup>53</sup>

$$\langle \Psi \rangle P_{\Psi}(\Psi) = \frac{\gamma}{\Gamma(\gamma)} \left( \frac{\gamma \Psi}{\langle \Psi \rangle} \right)^{\gamma-1} \exp\left( \frac{\gamma \Psi}{\langle \Psi \rangle} \right),$$
 (8)

with shape parameter  $\gamma = \tau_d/\tau_w$ , that is, the ratio of the pulse duration and the average pulse waiting time  $\tau w$ . This parameter describes the degree of pulse overlap, which determines the level of intermittency in the process. From the gamma distribution, it follows that the skewness moment is  $S_{\Psi} = \langle (\Psi - \langle \Psi \rangle)^3 \rangle / \Psi_{rms}^3 = 2/\gamma^{1/2}$  and the flatness moment is  $F_{\Psi} = \langle (\Psi - \langle \Psi \rangle)^4 \rangle / \Psi_{rms}^4 = 3 + 6/\gamma$ . Accordingly, there is a parabolic relationship between these moments given by  $F_{\Psi} = 3 + 3S_{\Psi}^2/2$ . For strong pulse overlap and large  $\gamma$ , the probability density function approaches a normal distribution and the skewness  $S_{\Psi}$  and excess flatness  $F_{\Psi} - 3$  moments vanish.

#### **III. PROFILES AND DISTRIBUTIONS**

The time-averaged electron density profiles in the turbulence simulations are presented in Fig. 5. Since the  $x_{SOL} = 50$  case does not include any sheath dissipation in the edge region, the average density is higher here than for the  $x_{SOL} = 0$  case. Throughout the SOL region,



**FIG. 5.** Time-averaged electron density profile for the  $x_{SOL} = 0$  and  $x_{SOL} = 50$  cases. The broken line is the best fit of an exponential function with a scale length of 35.5.

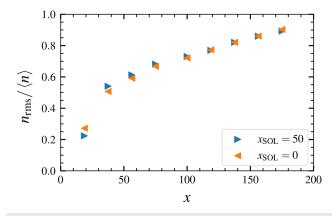
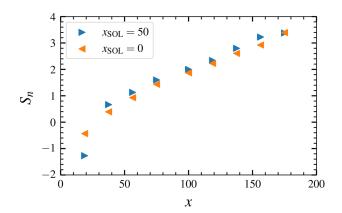


FIG. 6. The relative fluctuation level of the electron density at different positions in the SOL for the  $x_{SOL} = 0$  and  $x_{SOL} = 50$  cases.

we observe that the electron density decreases exponentially with a radially constant scale length of 35.5. This is to be compared with the equilibrium SOL profile scale length in the absence of turbulence given by  $\sqrt{D_{\perp}/\sigma_0} = \sqrt{20}$  for the simulation parameters used here.



**FIG. 7.** Skewness of the electron density fluctuations at different radial positions for the  $x_{SOL} = 0$  and  $x_{SOL} = 50$  cases.

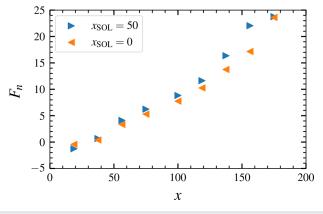
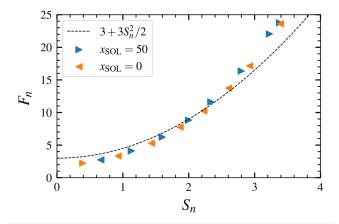


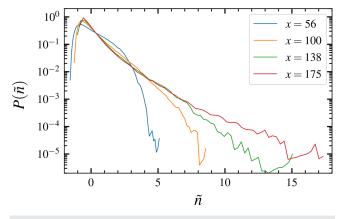
FIG. 8. Flatness of the electron density fluctuations at different radial positions for the  $x_{SOL} = 0$  and  $x_{SOL} = 50$  cases.

Interestingly, both the scale length and the absolute density are very similar for the two simulation cases investigated. We further show the relative fluctuation level at different radial positions for both cases in Fig. 6. The normalized fluctuation level is very high, increases radially outwards as the time-averaged density decreases faster than the absolute fluctuation level, and is roughly similar for the two simulation cases.

The radial variation of the skewness and flatness moments of the electron density fluctuations is presented in Figs. 7 and 8, respectively. From these figures, it is clear that the intermittency of the fluctuations increases radially outwards in the SOL, qualitatively similar for the  $x_{SOL} = 0$  and  $x_{SOL} = 50$  cases. By plotting the flatness moment vs the skewness, presented in Fig. 9, it is seen that for both simulation cases there is a nearly parabolic relationship between these higher order moments. The moments at x = 18.75 are not shown in Fig. 9 since they are measured close to the maximum amplitude of the source term. Such a parabolic relationship is predicted by the stochastic model describing the fluctuations as a superposition of uncorrelated pulses,<sup>43–46</sup> which can be related to blob-like structures moving radially outwards in the SOL as seen in Fig. 2.



**FIG. 9.** Flatness plotted vs skewness for the electron density fluctuations in the SOL. The broken line shows the parabolic relationship  $F_n = 3 + 3S_n^2/2$  for comparison.



**FIG. 10.** Probability density functions of the normalized electron density recorded at different radial positions for the  $x_{SOL} = 0$  case.

The PDFs for the normalized electron density fluctuations at different radial positions are presented in Figs. 10 and 11 for the  $x_{SOL}$ = 0 and  $x_{SOL}$  = 50 cases, respectively. The PDFs change from a narrow and nearly symmetric distribution in the edge/near SOL region to a distribution with an exponential tail for large fluctuation amplitudes in the far SOL. In Fig. 12, we further compare the PDFs of the electron density time series recorded in the far SOL at x = 100 for both simulation cases with a gamma distribution with a shape parameter of 1.4. Such a gamma distribution is predicted by the stochastic model describing the fluctuations as a superposition of uncorrelated exponential pulses. The gamma distribution is clearly an excellent description of the PDF for the electron density fluctuations in the simulations. A similar change in the shape of the PDF radially outwards in the SOL has also been reported from previous turbulence simulations.<sup>72–74</sup>

#### **IV. FLUCTUATION STATISTICS**

In this section, we present a detailed analysis of the electron density fluctuations recorded at x = 100. In order to reveal the typical shape of large-amplitude bursts in the time series, a conditional averaging method which allows for overlapping events is applied. This

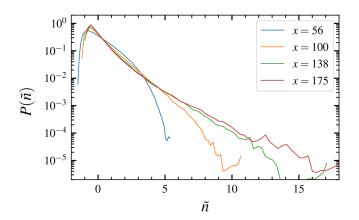
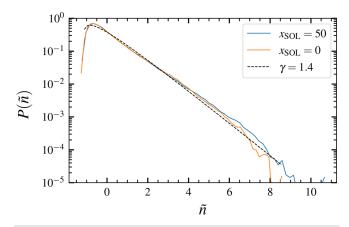


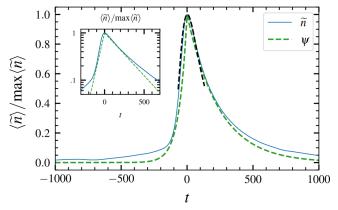
FIG. 11. Probability density functions of the normalized electron density recorded at different radial positions for the  $x_{\text{SOL}}=50$  case.



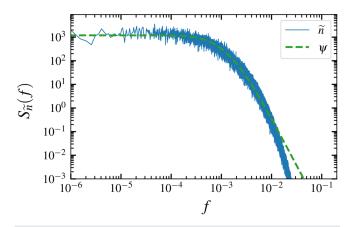
**FIG. 12.** Probability density functions of the normalized electron density recorded at x = 100 for both simulations cases compared to a gamma distribution with shape parameter  $\gamma = 1.4$  shown with the dashed black line.

identifies a total of 3128 conditional events with peak amplitudes larger than 2.5 times the root mean square value above the mean for the  $x_{SOL} = 50$  case and 1701 conditional events for the  $x_{SOL} = 0$  case. The average burst structures are presented in Fig. 13 and show an asymmetric shape with a fast rise and a slower decay. The burst shape is compared to an asymmetric, two-sided exponential function given by Eq. (6) with duration time  $\tau_d = 300$  and asymmetry parameter  $\lambda = 0.2$ . The conditional burst shape is shown with semilogarithmic axes in the inset in Fig. 13, showing that the decay of the conditional pulse shape is approximately exponential. However, the two-sided exponential function obviously fails to describe the smooth peak of the average burst shape in the simulations. As shown for short time lags in Fig. 13, this is better described using a skewed Lorentzian pulse as a fit function with duration 80 and skewness parameter 1 for the  $x_{SOL} =$ 50 case.<sup>87-90</sup> The slightly elevated tails of the conditional burst shape are likely due to finite pulse overlap in the turbulence simulations.

The frequency power spectral density due to a superposition of uncorrelated exponential pulses is compared to the simulation data of



**FIG. 13.** Conditionally averaged burst shape at x = 100 of the  $x_{SOL} = 50$  case (full blue line) compared to a two-sided exponential pulse (dashed green line), as well as a skewed Lorentzian pulse for short time lags (dashed black line). The conditional average is normalized by its peak amplitude.

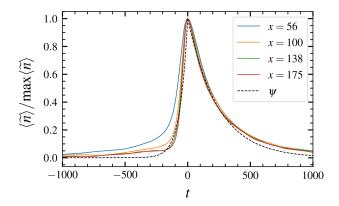


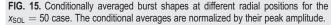
**FIG. 14.** Frequency power spectral density of the electron density fluctuations recorded at x = 100 for the  $x_{SOL} = 50$  case (full blue line). This is compared to the predictions of a stochastic model describing the fluctuations as a superposition of uncorrelated, two-sided exponential pulses with duration time  $\tau_d = 300$ , and asymmetry parameter  $\lambda = 0.2$  (dashed green line).

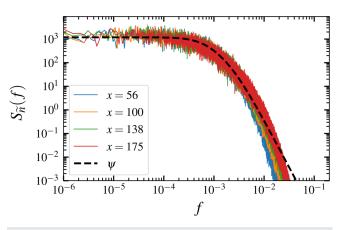
the electron density fluctuations recorded at x = 100 in Fig. 14 for the  $x_{SOL} = 50$  case. It is shown that the spectrum gives excellent agreement for high powers and low frequencies. Similar results for conditional averaging and frequency power spectra are found for the case  $x_{SOL} = 0$  but with slightly different pulse parameters.

The conditionally averaged burst shape is presented in Fig. 15 for different radial positions in the SOL for the  $x_{SOL} = 50$  case. Here it is seen that the burst shape in the far SOL region is the same for all radial positions, despite the fact that the relative fluctuation amplitude increases radially outwards. Accordingly, as predicted by the stochastic model, the frequency power spectral density has the same shape for all these different radial positions, as is shown in Figs. 16 and 17 for both the one- and two-region cases. The spectra are well described by that of a two-sided exponential pulse function, shown by the dashed black line in the figures.

Restricting the peak amplitude of conditional events in the electron density to be within a range of 2–4, 4–6, and 6–8 times the rms value, the appropriately scaled conditional burst shapes are presented in Fig. 18. This reveals that the average burst shape and duration do







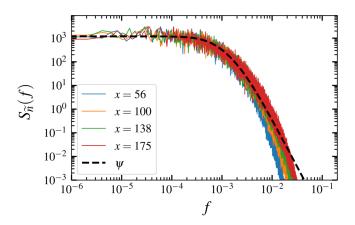
**FIG. 16.** Frequency power spectral densities of the electron density fluctuation recorded at different radial positions for the  $x_{SOL} = 50$  model. The dashed line shows the spectrum due to a superposition of uncorrelated, two-sided exponential pulses with duration time  $\tau d$ .

not depend on the burst amplitude and are again well described by a two-sided exponential function except for the smooth peak. This supports the assumption of fixed pulse duration in the stochastic model describing the fluctuations as a superposition of pulses.

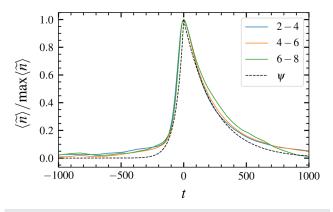
From the conditional averaging, we further obtain the peak amplitudes of conditional events and the waiting times between them. The PDFs of these are presented in Figs. 19 and 20, respectively. The distributions are similar for both simulation cases and are clearly well described by an exponential distribution as shown by the dashed black line in the plots. This is in agreement with the assumptions for the stochastic model presented in Sec. II. In particular, the exponential waiting time distribution supports the hypothesis that the events are uncorrelated and arrive according to a Poisson process.

#### V. DISCUSSION AND CONCLUSIONS

The abundant experimental evidence for universal statistical properties of fluctuations in the SOL of magnetically confined fusion



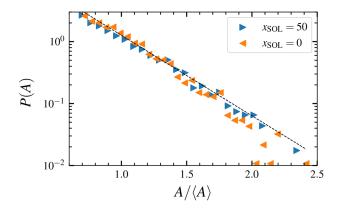
**FIG. 17.** Frequency power spectral densities of the electron density fluctuation recorded at different radial positions for the  $x_{SOL} = 0$  model. The dashed line shows the spectrum due to a superposition of uncorrelated two-sided exponential pulses.



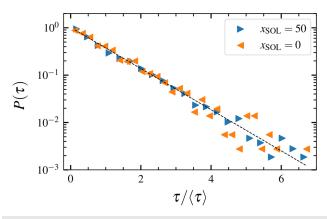
**FIG. 18.** Conditionally averaged burst shape at x = 100 of the  $x_{SOL} = 50$  case for different conditional amplitude threshold intervals. The conditional averages are normalized by their peak amplitudes.

plasmas sets high requirements for validation of turbulence simulation codes for the boundary region.<sup>54–56</sup> In this context, we have examined the statistical properties of the electron density fluctuations in the SOL by numerical simulations of plasma turbulence in the twodimensional plane perpendicular to the magnetic field. Two model cases have been considered: one describing resistive drift waves in the edge region and another including only the interchange instability due to unfavorable magnetic field curvature. For both cases, mushroomshaped blob-like structures move radially outwards, resulting in largeamplitude fluctuations and high average particle densities in the SOL. The numerical simulations show that the time-averaged radial profile decreases exponentially with radial distance into the SOL with the same characteristic length scale for both simulation cases. Moreover, the fluctuation statistics in the SOL are the same for both cases. This is despite the different linear instability mechanisms driving the fluctuations in the edge/near SOL region in the two simulation cases. It appears that any drift-ordered instability mechanism will lead to formation of filament structures when coupled to a SOL region with unfavorable magnetic field curvature.

According to a stochastic model describing the profile as due to radial motion of filament structures, the profile scale length is given by



**FIG. 19.** Probability density functions of conditional burst amplitudes of the electron density time series recorded at x = 100.



**FIG. 20.** Probability density functions of waiting times between consecutive largeamplitude burst in the electron density time series recorded at x = 100.

the product of the radial filament velocity and the parallel transit time.<sup>46–48</sup> This suggests that typical filament velocities are the same in both simulation cases. Future work will investigate the distribution of filament sizes and velocities by analysis of the velocity fluctuations and applying a blob tracking algorithm as described in Ref. 91.

The relative fluctuation level increases radially outwards, nearly reaching unity in the far SOL for the plasma parameters investigated here. Similarly, the skewness and flatness moments also increase into the SOL, and these higher order moments closely follow a quadratic dependence as predicted by the stochastic model describing the fluctuations as a superposition of uncorrelated pulses. The PDF of the electron density fluctuations changes from a nearly Gaussian distribution in the edge/near SOL region to a distribution with an exponential tail for large amplitudes in the far SOL. In the far SOL region, the PDFs are well described by a gamma distribution with the shape parameter given by the ratio of the pulse duration and average waiting time. The increase in this intermittency parameter with radial distance into the SOL suggests that only the most coherent and large-amplitude blob structures are able to move through the entire SOL region before they disperse and breakup due to secondary instabilities.

A conditional averaging analysis has revealed that the shape of large-amplitude bursts in single-point recordings in the far SOL is well described by a two-sided exponential pulse, as has previously been found in experimental measurements. Accordingly, the frequency power spectral density is well described by that of a two-sided exponential pulse for high powers and low frequencies. However, the high resolution and smoothness of the solution from the numerical computations imply that the burst structure has a rounded peak as opposed to the break point in experimental measurements due to their much lower sampling rate and additional measurement noise. The smooth peak is well described by a skewed Lorentzian pulse function. The frequency power spectral density therefore has an exponential decay for high frequencies and low powers with a slope that is given by the width of the narrow Lorentzian-shaped peak of large-amplitude fluctuations in the numerical simulations. In experimental measurements, this exponential tail in the spectrum may readily be masked by low sampling rates, limiting the highest frequencies resolved or by additive measurement noise, limiting the lowest power resolved.<sup>49,50</sup> The high frequency part of the power spectral density of the numerical

simulations therefore does not contradict experimental findings as these two counterparts cannot be directly compared.

In summary, it is here demonstrated that a simple but selfconsistent model for turbulent fluctuations in the scrape-off layer reveals the same statistical properties of large-amplitude events as found in the experiments. This includes exponentially distributed pulse amplitudes and waiting times, the latter supporting the assumption of Poisson events.<sup>28–33,36–40</sup> The simulation data also agree with predictions of the stochastic model, namely, an exponential average profile, gamma-distributed fluctuation amplitudes, and a frequency power spectral density determined by the average shape of largeamplitude bursts. It is concluded that the filtered Poisson process, describing the fluctuations in single-point recordings as a superposition of uncorrelated pulses with fixed duration, is an excellent description of the SOL plasma fluctuations in the turbulence simulations investigated here.<sup>43–53</sup>

The simple turbulence model used in this study does not include finite ion temperature effects, X-point physics, parallel collisional conductivity in the scrape-off layer, or any effect of interactions with neutral particles. Numerous SOL turbulence models and codes are now being extended to include these features.<sup>92–100</sup> The statistical framework with superposition of filaments can be used for analysis and interpretation of simulation results in these more advanced models, similar to what has been done here and previously for experimental measurements. As such, this work sets a new standard for validation of turbulence simulation codes.<sup>54–56</sup>

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#### DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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