

UKAEA

Preprint

STABILITY OF ANISOTROPIC PRESSURE TOKAMAK EQUILIBRIA TO IDEAL BALLOONING MODES

C. M. BISHOP R. J. HASTIE

CULHAM LABORATORY Abingdon Oxfordshire 1985 This document is intended for publication in a journal or at a conference and is made available on the understanding that extracts or references will not be published prior to publication of the original, without the consent of the authors.

Enquiries about copyright and reproduction should be addressed to the Librarian, UKAEA, Culham Laboratory, Abingdon, Oxon. OX14 3DB, England.

STABILITY OF ANISOTROPIC PRESSURE TOKAMAK EQUILIBRIA TO IDEAL BALLOONING MODES

C. M. Bishop and R. J. Hastie

Culham Laboratory, Abingdon, Oxon, OX14 3DB, England

(UKAEA/Euratom Fusion Association)

Abstract

The effect of pressure anisotropy on the stability of ideal mhd ballooning modes is studied for a large aspect ratio tokamak of circular cross section. Significant increase of the perpendicular energy of electrons or ions can cause strong modifications of the stability boundary, especially at low shear.

(Submitted for Publication in Nuclear Fusion)

1. Introduction

With the use of high power auxiliary heating in recent tokamak experiments there is evidence for the generation of pressure anisotropy. In TOSCA, for example, operating at densities of order $5 \times 10^{18} \text{m}^{-3}$ with ECR input power of 150 kW, poloidal asymmetry of the soft X-ray signal was observed [1], suggesting significant poloidal modulation of density or temperature, and possibly an increased population of energetic trapped electrons.

Neutral beam injection perpendicular to the field, and ICRH may be expected to modify the pressures in a similar way. Under these circumstances the distortions of the particle distribution functions from Maxwellian have two characteristics: (i) higher energy in the perpendicular direction and hence pressure anisotropy with $\rm p_{\perp} > p_{\parallel}$; (ii) the presence of a suprathermal tail.

Such distortions can modify mhd stability properties, particularly the β limit for ballooning instability. It is therefore of interest to determine (i) whether such modifications are favourable or unfavourable, and (ii) at what power level of the auxiliary heating, if any, they become significant.

The ballooning stability of anisotropic pressure tokamak equilibria has been investigated by Fielding and Haas [2,3], Cooper [4] and Mikhailovskii [5]. Fielding and Haas pointed out that stability could be improved relative to an isotropic plasma if nearly perpendicular neutral beam injection is employed to generate anisotropy in which the perpendicular pressure component is modulated in poloidal angle θ with maximum value on the <u>inside</u> of the tokamak minor cross section. Thus, with $\theta=0$ defining the outside, pressures of the form

$$p_{\parallel} = p_0(1 + \eta \cos \theta) \qquad \text{with } \eta < 0$$
 (1)

were found to enhance stability.

In reference [3] a model large aspect ratio, circular cross section

equilibrium in which B_{θ} is constant on a magnetic surface, was used. Cooper extended this work and confirmed the stabilising effect by studying the stability of global equilibria obtained from a numerical solution of the anisotropic Grad-Shafranov equation. In contrast Mikhailovskii found that excess perpendicular energy, $p_{\perp} > p_{\parallel}$ has a destabilising effect on ballooning and interchange modes in a large aspect ratio tokamak.

In this paper we extend these results and investigate the apparent conflict between references [3] and [5]. In section 2 the validity of the ideal mhd ballooning stability theory is briefly discussed. Section 3 is devoted to a description of the large aspect ratio equilibrium model, and the form of the stability equation for this model. In section 4 the results of numerical and analytic calculations of the stability boundaries are presented and these results are discussed and conclusions drawn in section 5.

2. Stability of Ballooning Modes

The ballooning stability of anisotropic tokamak equilibria is determined by the anisotropic ballooning equation [3,5]

$$\underline{B} \bullet \nabla \left\{ \frac{1}{R^{2}B_{p}^{2}} \left(1 + G^{2} \right) \underline{B} \bullet \nabla F \right\} + \frac{F}{RB_{p}} \left\{ K_{\psi} - GK_{s} \right\} \left\{ \frac{\partial}{\partial \psi} \left(p_{\parallel} + p_{\perp} \right) - \frac{B_{\phi}}{RB_{p}^{2}B} \frac{K_{\psi}}{K_{s}} \underline{B} \bullet \nabla \left(p_{\parallel} + p_{\perp} \right) \right\} = 0$$
(2)

where the magnetic field is defined by

$$B = I \nabla \phi - \nabla \phi \times \nabla \phi$$

and B and B denote the poloidal and toroidal components respectively. The distance to the axis of symmetry is R , the poloidal magnetic flux is ψ , and K are the principle and geodesic

curvatures:

$$K_{\psi} = \frac{\nabla \psi \cdot \nabla \left(p_{\perp} + \frac{1}{2} B^{2} \right)}{B^{2} (1 - \sigma) \left| \nabla \psi \right|}$$
(3)

$$K_{s} = \frac{\underline{B} \times \nabla \psi \cdot \nabla (\underline{p}_{\perp} + \frac{1}{2} \underline{B}^{2})}{\underline{B}^{3} (1 - \sigma) |\nabla \psi|}$$
(4)

with
$$\sigma = (p_{\parallel} - p_{\perp})/B^2$$
.

Finally the quantity G is defined by

$$G = \frac{R^2 B^2}{B} \int_{\chi_0}^{\chi} \frac{\partial}{\partial \psi} \left(\frac{IJ}{R^2}\right) d\chi \tag{5}$$

where χ is the poloidal coordinate with $\, \forall \chi \,$ orthogonal to $\, \forall \varphi \,$ and $\, \forall \psi$, and $\, J \,$ is the Jacobian.

Equation (2) was derived in references [3] and [4] by minimising the Kinetic Energy Principle of Kruskal and Oberman [6]. For plasmas with $p_{\parallel} > p_{\perp}$ it can be shown [7] that the kinetic term of this energy principle yields a small additional contribution of order $\epsilon^{3/2}$, where ϵ is the inverse aspect ratio. For the case of strong perpendicular anisotropy considered in this paper, the kinetic term may not be negligible, but provided the distribution function is monotonic in energy it can be shown to be positive definite. Its neglect, therefore, yields a sufficient condition for stability.

Another requirement must be satisfied in order that the use of equation (2) to study β limits be justified. This arises when some of the plasma pressure and pressure gradients are associated with a high energy, non-Maxwellian, tail in the particle distribution. When such high energy particles are present, equation (2) still provides a valid stability test provided that the mode frequency at marginal stability exceeds the toroidal precession frequency of such energetic trapped particles. Finite larmor radius effects determine the frequency at marginal stability to be

$$\omega = \frac{1}{2} \omega_{*p_{i}}$$

where $\omega_{*p_{\dot{1}}}=\frac{\ell}{Ne_{\dot{1}}}\frac{dp_{\dot{1}}}{d\varphi}$ with ℓ the toroidal mode number. Thus the condition becomes

$$\frac{1}{2} \omega_{*p_{i}} > \langle \omega_{d} \rangle$$

where $<\!\omega_{\!\!\!\!d}\!>$ is the precession frequency of the energetic particles. This is effectively a constraint on the energy W of such suprathermals and is equivalent to

$$\frac{W}{kT} < \varepsilon^{-1}$$
 (6)

When this condition is violated, it has been shown [8] that the suprathermal particles have a stabilising effect, and that higher β values can be attained than equation (2) would predict.

The calculations presented here assume that the inequality (6) is satisfied so that all parts of the electron and ion distributions behave in a fluid-like manner.

Equilibrium Model

The equilibrium is calculated locally, following Mercier and Luc [9], by expansion around a magnetic surface. For an isotropic equilibrium this method requires the specification of the shape of the magnetic surface and the variation of the poloidal magnetic field, $B_{\rm p}$, around the surface. We shall consider a large aspect ratio equilibrium with strong perpendicular anisotropy, i.e. $C/B^2 = O(1)$ in the aspect ratio expansion, where

$$C = 4\pi \sum_{j} m_{j} \int \frac{B}{|v_{\parallel}|} (\mu B)^{2} \frac{\partial F_{j}}{\partial K} d\mu dK$$
 (7)

where μ and K are the magnetic moment and particle energy per unit mass respectively. In this case it is necessary to specify, in addition, the variation of both $~p_{\perp}~$ and $~\partial p_{\perp}/\partial \psi~$ around the surface.

The equilibrium is determined by the following conditions

- (a) Large aspect ratio: ϵ << 1.
- (b) $\beta_{\parallel} \sim \beta_{\parallel} \sim \epsilon$.
- (c) Circular magnetic surface.
- (d) Variation of $\begin{array}{ccc} B & \text{round the surface specified.} \\ p & \end{array}$
- (e) C/B² ~ .O(1) and therefore finite variation of p and $\partial p_{\perp}/\partial \psi$ round the magnetic surface.

A consequence of the conditions (a) and (b) above follows from the equilibrium relation $\dot{}$

$$\underline{\mathbf{B}} \bullet \nabla \mathbf{p}_{\parallel} + \frac{\mathbf{p}_{\perp} - \mathbf{p}_{\parallel}}{\mathbf{B}} \; \underline{\mathbf{B}} \bullet \nabla \mathbf{B} = 0 \quad , \tag{8}$$

namely that the variation of p_{\parallel} and $\delta p_{\parallel}/\delta \psi$ around the surface is of order ϵ . The O(ϵ) modulation of $\left(\frac{\delta p_{\parallel}}{\delta \psi}\right)_{\chi}$ round the magnetic surface is nevertheless required in the stability calculation and is obtained explicitly from equation (8).

To simplify the ballooning equation a convenient variable is the poloidal angle, θ , defined in terms of $\,\chi\,$ by:

$$\theta = \int_{-\infty}^{\chi} \frac{JB}{r} d\chi \tag{9}$$

where r is the radius of curvature of the magnetic surface under consideration. Since we assume this surface is circular r is independent of $\,\theta$.

Using the large aspect ratio expansion and $~\beta\sim\epsilon~$ ordering, the curvatures $K_{_{\textstyle \psi}}$ and $K_{_{\textstyle S}}$ can be evaluated to leading order in $~\epsilon~$ to give

$$K_{\psi} = -\frac{\cos\theta}{R_0} \tag{10}$$

$$K_{S} = \frac{\sin \theta}{R_{0}} \tag{11}$$

where $R = R_0 + r\cos\theta$.

The ballooning equation (2) now takes the form

$$B_{p} \frac{\partial}{\partial \theta} \left\{ \frac{1}{B_{p}} \left(1 + G^{2} \right) \frac{\partial F}{\partial \theta} \right\}$$

$$- \frac{r^{2}}{B_{p}} F \left\{ \cos \theta + G \sin \theta \right\} \left\{ p_{\parallel}' + p_{\perp}' + \frac{\cos \theta}{\sin \theta} \frac{\partial p_{\parallel}}{\partial \theta} \frac{1}{R_{0} r B_{p}} \right\} = 0 \qquad (12)$$

where
$$p'_{\parallel} = \frac{\partial p_{\parallel}}{\partial \phi}$$
 and $p'_{\perp} = \frac{\partial p_{\perp}}{\partial \phi}$.

Making use of the aspect ratio expansion, the expression for $\, {\tt G} \,$ may be simplified to the form

$$G = -RrB_{p}^{2} \int_{\theta_{0}}^{\theta} \frac{d\theta}{B_{p}^{3}} \left\{ \frac{\partial B_{p}^{2}}{\partial \psi} + (1 - \sigma) \frac{\partial P_{\parallel}}{\partial \psi} + \frac{LL'}{R^{2}} \right\}$$
(13)

where L(ψ) = I(1 - σ) , and $\partial B^2/\partial \psi$ may be obtained from a local solution of the Grad-Shafranov equation with the result

$$\frac{\partial B_{p}^{2}}{\partial \psi} = -2 \left\{ \frac{B_{p}}{Rr} + (1 - \sigma) \frac{\partial P_{\parallel}}{\partial \psi} + \frac{LL'}{R^{2}} \right\} . \tag{14}$$

In equations (13) and (14) the small terms $\sigma \frac{\partial p_{\parallel}}{\partial \psi}$ and $\frac{\partial p_{\parallel}}{\partial \psi}$ and $\frac{\partial p_{\parallel}}{\partial \psi} + \frac{LL'}{R_0^2}$. The

order ϵ correction to $\frac{\partial p_{\parallel}}{\partial \psi}$ is also required and to determine this we introduce explicit forms for $p_{\perp}(\theta)$, $\frac{\partial p_{\perp}}{\partial \psi}(\theta)$, $p_{\parallel}(\theta)$ etc. Thus we take

$$\begin{aligned} \mathbf{p}_{\perp} &= \mathbf{p}_{\perp_0} (1 + \eta \cos \theta) \\ \frac{\partial \mathbf{p}_{\perp}}{\partial \phi} &= \mathbf{p}_{\perp_0}' (1 + \eta \cos \theta) \\ \\ \mathbf{B}_{\mathbf{p}} &= \mathbf{B}_{\mathbf{p}_0} / \mathbf{g}(\theta) \quad ; \quad \mathbf{g}(\theta) = 1 - \Lambda \cos \theta \\ \\ \mathbf{p}_{\parallel} &= \mathbf{p}_{\parallel_0} + O(\epsilon) \\ \\ \frac{\partial \mathbf{p}_{\parallel}}{\partial \phi} &= \mathbf{p}_{\parallel_0}' + O(\epsilon) \end{aligned}$$

The parameter Λ represents the effect of the outward shift of the magnetic surfaces in toroidal equilibrium – the Shafranov shift. The degree of anisotropy is controlled by the parameters $\begin{pmatrix} p_{\downarrow_0} - p_{\parallel_0} \end{pmatrix}$, $\begin{pmatrix} p_{\downarrow_0}' - p_{\parallel_0}' \end{pmatrix}$ and η .

Since we are particularly interested in the effect on stability of poloidal variation of the perpendicular pressure $(\eta \neq 0)$ we simplify the equilibrium model by choosing $p_{\parallel_0} = p_{\perp_0} \equiv p_0$, $p'_{\parallel_0} = p'_{\perp_0} \equiv p'_0$.

The small modulation in θ of $\Big(\frac{\partial p}{\partial \psi}\Big)$ is now obtained from equation (8) and found to be

$$\left(\frac{\partial p_{\parallel}}{\partial \psi}\right)_{1} = \frac{\eta \varepsilon}{4} \cos 2\theta \left\{ p_{0}' \left(1 + \frac{\eta \beta}{\varepsilon}\right) + \frac{p_{0}}{R_{0} r_{p_{0}}^{B}} \right\} - \frac{\eta \varepsilon p_{0} \Lambda}{2R_{0} r_{p_{0}}^{B}} \left\{ \cos \theta + \frac{1}{3} \cos 3\theta \right\} .$$
(15)

The parameter $p_0' + LL'/R_0^2$ is then eliminated from the expression for G (equations (13) and (14)) in favour of the global shear, s, defined by

$$s = \frac{R_0 r B_{p_0}}{q} \frac{dq}{d\psi}$$
 (16)

with q the safety factor.

The ballooning equation then takes the form

$$\frac{\partial}{\partial \theta} \left\{ g(\theta) (1 + G^2) \frac{\partial F}{\partial \theta} \right\}$$

$$+ g^2 F \left\{ \cos \theta + G \sin \theta \right\} \left\{ \alpha + \frac{\alpha \eta}{2} \cos \theta + \frac{\eta \beta q^2}{2\epsilon} g \cos \theta \right\} = 0$$
 (17)

where
$$\alpha = -2R_0^2 \frac{B_{p_0} p_0' q^2}{B^2}$$
; $\beta = \frac{2p_0}{B^2}$

and

$$g^{2}G = s(\theta - \theta_{0}) + 2 \int_{\theta_{0}}^{\theta} \left[g^{2}\right] d\theta - \alpha \left(1 + \frac{\eta \beta}{4\epsilon}\right) \int_{\theta_{0}}^{\theta} \left[g^{3} \cos \theta\right] d\theta$$

$$- \frac{\eta}{8} \left\{\alpha \left(1 + \frac{\eta \beta}{\epsilon}\right) - \frac{\beta q^{2}}{\epsilon}\right\} \int_{\theta_{0}}^{\theta} \left[g^{3} \cos 2\theta\right] d\theta - \frac{\eta \beta q^{2} \Lambda}{3\epsilon} \int_{\theta_{0}}^{\theta} \left[g^{3} \cos^{3}\theta\right] d\theta$$

$$+ \frac{Q}{\langle g^{3} \rangle} \int_{\theta_{0}}^{\theta} \left[g^{3}\right] d\theta \qquad (18)$$

where

$$Q = s - 2\langle g^2 \rangle + \alpha \left(1 + \frac{\eta \beta}{4\epsilon}\right)\langle g^3 \cos \theta \rangle + \frac{\eta}{8} \left\{\alpha \left(1 + \frac{\eta \beta}{\epsilon}\right) - \frac{\beta q^2}{\epsilon}\right\}\langle g^3 \cos 2\theta \rangle + \frac{\eta \beta q^2 \Lambda}{3\epsilon} \langle g^3 \cos^3 \theta \rangle$$

$$(19)$$

and the bracket notations in equations (18) and (19) are defined by:

$$\langle x \rangle = \frac{1}{2\pi} \oint x d\theta$$
 , $[x] = x - \langle x \rangle$.

If the poloidal magnetic field is constant round a magnetic surface (i.e. $\Lambda=0$) then in equation (17)

$$G \rightarrow s(\theta - \theta_0) - \alpha \left(1 + \frac{\eta \beta}{4\epsilon}\right) (\sin \theta - \sin \theta_0)$$

$$- \frac{\eta}{16} \left\{\alpha \left(1 + \frac{\eta \beta}{\epsilon}\right) - \frac{\beta \alpha^2}{\epsilon}\right\} (\sin 2\theta - \sin 2\theta_0) . \tag{20}$$

If the further limit $\beta/\epsilon \to 0$ is taken, equation (17) reduces to the ballooning equation solved in reference [3], while if the isotropic limit, $\eta \to 0$, is taken, equation (17) reduces to the $(s-\alpha)$ equation of Connor et al [10].

4. Stability Boundaries for Interchange and Ballooning Modes

We first note that the criterion for mirror stability,

$$\{\underline{\mathbf{B}} \bullet \nabla (\mathbf{p}_{\perp} + \frac{1}{2} \mathbf{B}^{2})\} \{\underline{\mathbf{B}} \bullet \nabla \mathbf{B}\} > 0$$
 (21)

takes the form

$$1 + \frac{\eta \beta}{25} > 0$$
 (22)

for the equilibria considered in the previous section. Instability is therefore only possible for rather large values of β/ϵ and for negative values of η (p larger on the inside of the tokamak cross-section).

Stability to interchange modes is determined by the Mercier criterion [11] which is obtained from the asymptotic behaviour of the ballooning equation. When $\Lambda \neq 0$ the resulting criterion is complicated and has been evaluated numerically for the stability diagrams presented below. When $\Lambda = 0$, however, it takes the relatively simple form:

$$s^{2} > \eta \left\{ \alpha + \frac{\beta q^{2}}{\varepsilon} - \frac{1}{2} \frac{\alpha^{2} \beta}{\varepsilon} + \frac{\eta}{16} \left(\alpha + \frac{\beta q^{2}}{\varepsilon} \right) \frac{\beta q^{2}}{\varepsilon} \left(1 - \frac{\eta \alpha}{2q^{2}} \right) \right\} . \tag{23}$$

For small values of α and $\beta q^2/\epsilon$, positive values of η are seen to be destabilising. The term $\eta\alpha$ on the right hand side of the inequality arises because of the weighting of the radial pressure gradient towards the unfavourable curvature region. This effect is however reinforced by the longitudinal pressure gradient appearing as $\eta\beta q^2/\epsilon$. For negative η values these effects are stabilising so that interchange modes were not unstable for the inward shifted p_{\parallel} surfaces of Fielding and Haas.

The destabilising effect of pressure weighting towards the unfavourable curvature also applies to ideal ballooning modes. These modes are now required to 'balloon' less and hence cause less field line bending with its consequent stabilising effects.

In Fig 1 the stability boundaries in an $s-\alpha$ diagram are shown for $\beta/\epsilon=0$ and several values of η . Fig 2 shows the destabilising effect of longitudinal pressure gradients, $\beta/\epsilon\neq0$, on the stability boundaries when $\eta=0.5$. In both figures the interchange stability boundaries are included, and are seen to be important for small shear.

In Fig 3 we show the largely stabilising effect of the outward toroidal equilibrium shift, Λ = 0.25 , for an isotropic plasma, while Fig

4 shows the result of the competing influence of the equilibrium shift and unfavourable pressure weighting (positive η).

In Fig 5 we show the marked effect of unfavourable pressure weighting on the second stability region, and for comparison the favourable effect of inward shifted pressure surfaces. This shows the sensitivity of the ballooning instability to modulation of the perpendicular pressure round a magnetic surface.

Discussion of Results

From the foregoing results it is clear that auxiliary heating methods which generate 'strong perpendicular anisotropy', ie finite poloidal variation of $p_{\perp}(\theta)$, will have a significant effect on the critical pressure and pressure gradient for ballooning instability. This is especially true in regions of low magnetic shear s . Fielding and Haas found that for an inward shift of the $p_{\perp}'=$ const surfaces ($\eta<0$ in the previous section) the first and second stability regions coalesce for low shear. The result of the present investigations is that for $\eta>0$ interchange modes become unstable at low shear. In addition we find that the effect of the longitudinal pressure gradient coupled to the goedesic curvature reinforces the stabilising or destabilising effects associated with the poloidal variations of the radial pressure gradient.

In regions of stronger shear the destabilising effect of positive $\ensuremath{\eta}$ persists, but is weaker.

These effects are quite distinct from the destabilisation found by Mikhailovskii. The anisotropic equilibria studied by Mikhailovskii differ from those studied here in the ordering in the aspect ratio parameter $\epsilon=a/R$, of the pressure-like moment C defined by equation (7). The finite modulation of $p_{\perp}(\theta)$, in equation (1), implies that $C/B^2\sim O(1)$. In reference [5] the ordering

$$\frac{p_{\parallel}}{B^2} \sim \frac{p_{\perp}}{B^2} \sim \frac{c}{B^2} \lesssim O(\epsilon)$$

is taken. For such equilibria both components of the pressure are constant round the magnetic surface in leading order in ϵ , so $\eta=0$. The degree of anisotropy in this case is measured by the parameters $\left(p_{\perp_0}-p_{\parallel_0}\right)$, and $\left(p_{\perp_0}'-p_{\parallel_0}'\right)$.

If in section 4 we had taken $p_{\parallel_0} \neq p_{\perp_0}$, $p'_{\parallel_0} \neq p'_{\perp_0}$ the interchange stability criterion becomes (when Λ = 0)

$$s^{2} > \overline{\alpha} \left(\frac{\beta_{\perp} - \beta_{\parallel}}{\varepsilon} \right) q^{2} + \eta \left\{ \alpha_{\perp} + \beta_{\perp} q^{2} / \varepsilon - \overline{\alpha} \alpha_{\perp} \left(\beta_{\perp} - \frac{1}{2} \beta_{\parallel} \right) / \varepsilon \right.$$

$$\left. + \frac{\eta}{64} \frac{\beta q^{2}}{\varepsilon} \left(\alpha_{\perp} + \frac{\beta_{\perp} q^{2}}{\varepsilon} \right) \left(1 - \frac{\eta \alpha_{\perp}}{2q^{2}} \right) \right\}$$

where

$$\bar{\alpha} = -R_0^2 B_p (p'_{\parallel_0} + p'_{\perp_0}) q^2 / B^2 ; \quad \alpha_{\perp} = -2R_0^2 B_p p'_{\perp_0} q^2 / B^2$$

$$\beta_{\perp} = 2p_{\perp_0} / B^2 ; \quad \beta_{\parallel} = 2p_{\parallel_0} / B^2 .$$

Here the first term on the right hand side shows the destabilising effect of $\beta_{\|}>\beta_{\|}$ found by Mikhailovskii.

We conclude that two parameters characterising the anisotropy of a tokamak with auxilliary heating are of importance in assessing the effect of anistropy on ballooning stability and therefore β limits. These are $\left(p_{\perp}-p_{\parallel}\right)/p_{\parallel}$, and $\left\{p_{\perp}(\theta=0)-p_{\perp}(\theta=\pi)\right\}/p_{\perp}(\theta=\pi)$ which is a measure of the parameter η of the foregoing study. In optimising the parameters of any heating scheme one desirable feature ought to be the achievement of small or negative η values.

Acknowledgement

We are indebted to T. J. Martin for the numerical evaluation of the Mercier stability boundaries in Fig 4.

References

- [1] ROBINSON, D.C., ALCOCK, M.W., AINSWORTH, N.R., LLOYD, B., MORRIS, A.W. Proc. of the 3rd Joint International Symposium on Heating in Toroidal Plasmas, Grenoble, 1982, Vol II, 647.
- [2] FIELDING, P.J., HAAS, F.A. Phys. Rev. Letts. 41 (1978) 801.
- [3] SYKES, A., TURNER, M.F., FIELDING, P.J., HAAS, F.A. Proc. of the 6th Int. Conf. on Plasma Physics and Controlled Nuclear Fusion, Innsbruck, Vol I, IAEA, Vienna (1979) 625.
- [4] COOPER, W.A., BATEMAN, G., NELSON, D.B., KAMMASH, T. Plasma Physics 28 (1981) 105.
- [5] MIKHAILOVSKII, A.B., Soviet Journal of Plasma Physics 8 (1982) 477.
- [6] KRUSKAL, M.D., OBERMAN, C.R. Phys. Fluids 1 (1958) 275.
- [7] RUTHERFORD, P.H., CHEN, L., ROSENBLUTH, M.N. Princeton University, Plasma Physics Laboratory, Report PPPL-1418 (1978).
- [8] ROSENBLUTH, M.N., TSAI, S.T., VAN DAM, J.W., ENQUIST, M.G. Phys. Rev. Letts. 51 (1983) 1967
- [9] MERCIER, C., LUC, N. MHD Approach to Confinement in Toroidal Systems, Commission of the European Communities, Brussels, Report EUR-5127e (1974).
- [10] CONNOR, J.W., HASTIE, R.J., TAYLOR, J.B. Phys. Rev. Lett 40 No 6 (1978) 396.
- [11] MERCIER, C. Nucl. Fusion 1 (1960) 47.



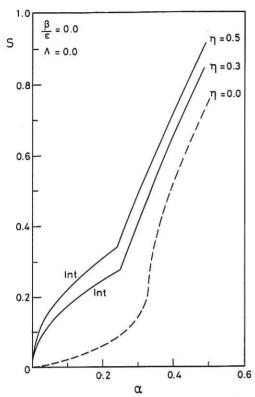


Fig.1 Effect of pressure anisotropy on the $s-\alpha$ stability boundary. In this and subsequent figures "Int" denotes the part of the stability boundary due to interchange modes.

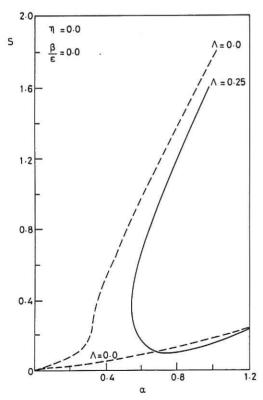


Fig. 3 Effect of an outward toroidal shift in an isotropic plasma.

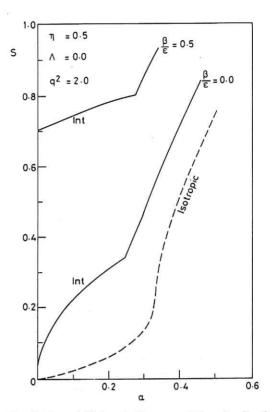


Fig. 2 Destabilising influence of longitudinal pressure gradients.

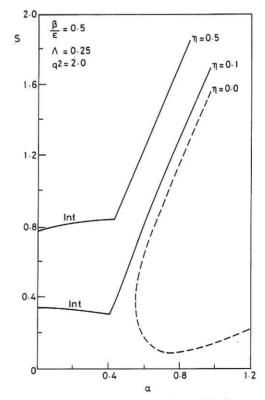


Fig. 4 Competing influence of equilibrium shift and unfavourable pressure modulation.

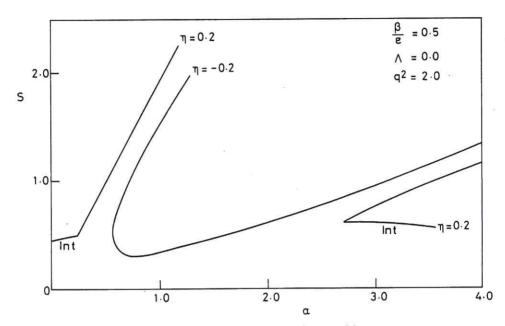


Fig. 5 Effects of favourable and unfavourable pressure modulation on the second stability region.



