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Towards DEMO Concept Selection Under Epistemic Uncertainty

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Towards DEMO Concept Selection Under Epistemic Uncertainty

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Abstract—To make informed decisions during the concept selection activities of a fusion power plant it is necessary to evaluate the impact of uncertainties on the feasibility and performance of each concept. A framework for uncertainty quantification and sensitivity analysis has been developed for the PROCESS systems code to allow the direct comparison of different DEMO concepts. To account for epistemic uncertainty, the uncertainty quantification was based on interval analysis, where only the bounds of the interval have to be assumed for each uncertain parameter, and the uncertainty was propagated with Monte Carlo and Latin Hypercube Sampling. The sensitivity analysis was based on the pinching method, consisting in reducing the interval uncertainty of each input parameter to a baseline point one by one, and measuring the uncertainty reduction in the output interval. Its application is shown using the European H-mode DEMO baseline as a use case. Results suggest that the thermal He-4 fraction in plasma, plasma elongation, and H-factor should be examined further to reduce risks on its feasibility.

Index Terms—DEMO, PROCESS, uncertainty quantification, sensitivity analysis

I. INTRODUCTION

Despite having built successful fusion reactors in the past, the design and development of a fusion power plant presents an unparalleled challenge, since it is technically and economically prohibitive to build and test every single concept that is under investigation. However, digital models can help to mitigate this problem. With the recent advances in computer-aided modeling, now it is possible to build virtual prototypes to study and assess concepts before turning them into a reality. Fusion systems codes, such as PROCESS [1], [2], serve as a tool to perform the initial approach towards a fusion power plant concept, helping to evaluate its performance before narrowing down its operational space with more detailed and sophisticated codes [3].

With uncertainty quantification methods, it is possible to determine outcomes from a concept when some aspects of it are unknown. This application is particularly useful to quantitatively assess concept choices early in the design process, and to identify areas with high impact on the performance

of the concept of choice that need further development to meet the requirements or could pose a risk for finding a successful concept. Some previous work has been carried out in uncertainty quantification with PROCESS; on the European DEMO as in [4]–[6], on the CFETR design [7], or the HELIAS 5-B stellarator [8].

For decades the high confinement, or H-mode, has been considered the preferable plasma operation regime for a fusion power plant [9]. However, after revisiting the potential impact of the type-I ELMs associated with H-mode plasmas, new plasma operational scenarios have been proposed as an alternative [10]. Therefore, to allow comparison among DEMO concepts using different plasma scenarios, it is of paramount importance to design methodologies and metrics that:

- 1) Help to assess how the current state of knowledge affects to each DEMO concept;
- 2) Help to identify which areas of knowledge are required to be sharpened to make different DEMO concepts successful.

In this paper we present a framework for uncertainty quantification and sensitivity analysis to perform concept selection, and its application is shown with the European H-mode DEMO baseline as a use case.

II. UNCERTAINTY

There are two kinds of uncertainties: aleatory and epistemic. If the distribution function of a random variable is perfectly known, then the stochastic nature of the random variable is fully captured by this distribution function, and the uncertainty is said to be aleatory - it is random by nature, but not uncertain. However, when the distribution function cannot be precisely defined, because the information available (data) does not allow it, then this imprecision is called epistemic uncertainty, which arises from lack of knowledge about that random variable, and therefore it should be reducible with additional information.

Despite there is a long lasting debate on how to model imprecision [11], [12], the framework developed in this work used intervals to model epistemic uncertainties, since the DEMO design parameters are not stochastic by nature, but uncertain. Intervals represent the least amount of useful knowledge, since only the bounds of the interval have to be assumed for each uncertain parameter.

Only six parameters were considered for this work, yet it is possible to increase this number in exchange of a greater computational cost. Sensitivity analysis will help to refine the parameter selection, aiding to discard those parameters that have little or no impact on the uncertainty of the output. The parameters chosen were related to the physics in PROCESS rather than technological (such as efficiencies), as the next step attempts to understand how these uncertainties impact on the different plasma scenarios. To maintain similarity with previous studies, these parameters are present in [6], and were:

- H-factor $\in [1.0, 1.3]$: the ratio between measured energy confinement time and the predicted energy confinement time by the ITERH-9P(y,2) scaling law [13]. Values greater than 1.3 are not expected to be achievable [14].
- Divertor operational limit $\in [8.7, 9.5] \frac{MWT}{m}$: the maximum power allowed to cross the separatrix and flow on the divertor plates. It is unknown what will be the limit at the time of construction of DEMO, but current concepts aim for $\sim 9 \frac{MWT}{m}$.
- Core radius energy confinement time scaling $\in [0.6, 0.8]$: the energy confinement scaling law has been derived from experiments with low radiation (i.e. without significant radiation inside the separatrix). DEMO is expected to operate with high radiation scenarios [15], and the parameter representing the fraction of radiation that is released from the core has to be adjusted accordingly.
- Tungsten impurity fraction $\in [10^{-5}, 10^{-4}]$: high-Z impurities generated from the interaction of plasma with plasma facing components lead to losses in energy confinement time due to radiative processes. The amount of tungsten concentration in DEMO during operation is still uncertain, and it is unknown how these impurities will be removed.
- Plasma elongation $\in [1.75, 1.90]$: elongation is the dominant plasma parameter and has been reported as having the largest impact on the net electric power of the machine [6]. In conventional tokamaks, an elongation of over 2 is not expected to be controllable, and an elongation smaller than 1.70 could yield poor performances [16].
- Thermal He-4 fraction $\in [0.06, 0.12]$: Helium-4 is one of the products of the DT fusion reaction, and it is a positively charged particle intended to stay confined in the plasma. It has the role of keeping the energy confinement high enough to sustain the fusion reactions, and minimising the amount of external heating required. On the other hand, if its concentration in the plasma is too high, it dilutes the fuel and diminishes the fusion power; therefore, an optimal solution must exist

where both confinement time and fusion power conditions are satisfied. This fraction is highly variable in current transport simulations, and most of the plasma physics experiments were conducted without these ions, so the fraction of it in DEMO plasmas is uncertain.

The uncertain input parameters, with their respective interval and baseline value are summarised in Table 1.

TABLE I
PARAMETERS USED FOR THE ANALYSIS, WITH THEIR ASSOCIATED UNCERTAINTY IN THE FORM OF INTERVAL AND BASELINE VALUE.

Parameter	Lower bound	Upper bound	Baseline
H-factor	1.0	1.3	1.1
Divertor Limit (MWT/m)	8.7	9.5	9.2
Core Radius	0.6	0.8	0.75
W Impurity	10^{-5}	10^{-4}	50^{-5}
Plasma Elongation	1.75	1.90	1.85
Thermal He-4 fraction	0.06	0.12	0.069

III. METHODS

The proposed methodology is based on interval analysis [17], consisting in defining the uncertain parameters as intervals, and performing the model simulation to find the minimum and maximum of the output. Due to the size and complexity of PROCESS, this analysis cannot be performed via intrusive methods (i.e. implementing interval arithmetic in the code), which would provide the rigorous output interval.

Fortunately, PROCESS is built with 0-1D models and therefore runs relatively fast (e.g. a single PROCESS run finishes in a few seconds on an ordinary laptop). For this reason, sampling (also called brute-force search) was chosen as the method to obtain the output interval. Also, sampling allows the identification of trends or patterns (such as nonlinearities, discontinuities, dependencies, etc.) in the data, which can be useful to perform sensitivity analysis. For this work, the European H-mode DEMO baseline is modeled in PROCESS, set to minimise the major radius (R_0) constrained with at least 400 MW of net electric power and a pulse length of 2 hours.

Uncertainty quantification should be accompanied with a sensitivity analysis because analysts and decision-makers are interested not only in the amount of uncertainty on the model output, but also on how do the input parameters uncertainties affect to it. Two different approaches were taken to perform sensitivity analysis: one qualitative, visualising the scatterplots generated with the data previously used to perform uncertainty quantification [18], and one quantitative, based on the pinching method, consisting in reducing the interval uncertainty of each input parameter to a baseline point one by one, and measuring the uncertainty reduction in the output interval [19].

A. Uncertainty Quantification

Major radius (R_0) was chosen as the model output of interest, as it is one of the main drivers of the power plant size, indicator of cost and overall feasibility. It would be desirable to have the major radius interval as narrow as possible, which would mean that for the given input parameters uncertainties,

the size of the machine is definite. For example, assuming that the maximum major radius permitted is 12 metres, then if the major radius interval of a specific DEMO concept is [12.3, 12.4] metres, then it would be sensible to classify that concept as unfeasible, since its major radius would be too large. On the other hand, if the major radius interval is [8.5, 8.6] metres, then that concept should be considered as a feasible option, since its major radius will always be under 12 metres.

Worst case scenario happens when the major radius interval is too wide to make a decision, as [8.5, 12.4] metres would be. In this case, for the given values of the uncertain input parameters, the major radius could be any within that interval, and therefore one could not classify that concept as feasible or unfeasible. However, a wide interval is not necessarily a bad result; it means that it is required to reduce the amount of uncertainty in input parameters to be able to make a decision.

For DEMO concept selection, the distance of the major radius interval ($b - a$ where $R_0 \in [a, b]$) is used as a concept robustness metric, meaning that the smaller the distance, the more robust the concept is (i.e. the input parameters uncertainties have less impact on the size uncertainty of the reactor).

The sampling method chosen to perform the analysis was Latin Hypercube Sampling (LHS), which is generally recommended in the literature, as it stratifies over the range of each interval input, making possible to perform both uncertainty and sensitivity analysis [18].

In LHS, the distribution function of each input parameter X_k is equally divided N times with the same marginal probability $1/N$, where N is the number of desired samples. This division will ensure that the distribution function is properly sampled, as it will avoid repetition of points or missing regions of the function. Then, the algorithm takes only one sample from each division, and repeats the process for all the input parameters, to later ensemble randomly the taken samples, and form the input sets. For this analysis, 6600 samples were employed, which are enough to cover the whole parameter space [20].

It is important to recall that in order to generate the samples of the uncertain input parameters, LHS requires to assume a probability density function. A uniform distribution was chosen for the uncertain input parameters, with range being equal to their respective interval, since this distribution stratifies equally through the whole interval and no preference is given to any region of the interval. However, this step is only required for the sampling, and no probabilistic interpretation should be drawn from the analysis, since it would be an artifact of the sampling.

B. Sensitivity Analysis

The objective of sensitivity analysis is to study how the uncertainty in the output of a model is influenced by the uncertainties of its inputs. Its application in concept selection studies is twofold:

- 1) In the presence of different DEMO concepts, clarify how parameter uncertainty affects the confidence in the outcome of each concept;
- 2) Identify parameters that would require resources invested to reduce uncertainty and achieve a suitable degree of confidence on each concept.

Two model outputs were analysed for this work: major radius and feasibility. The PROCESS systems code has an output variable which returns whether PROCESS found a feasible solution or not. PROCESS returns a feasible solution when, for a given set of input variables and design parameters, all the model constraints are fulfilled. However, if PROCESS cannot find a solution with all the model constraints fulfilled, then it returns the run as unfeasible. This metric is particularly interesting because it can help to identify operational regions that could be problematic to integrate or cannot be achieved.

When the uncertainty on the output of the model has been calculated using sampling methods, the simplest procedure to perform sensitivity analysis is examining the scatterplots associated with the input parameters and the model output [18]. In the case a parameter has significant effect on the major radius, then it should show a discernible pattern on its corresponding scatterplot. These plots have been accompanied with a weighted linear regression to help visualise trends in data.

To enhance the robustness on the suggestions of the scatterplots, a more quantitative method for local sensitivity analysis based on Value-of-Information is also carried out [21]. Its objective is to measure the reduction of uncertainty on the output if extra knowledge about the inputs is acquired. The initial step is to calculate the output uncertainty with all the input parameters being uncertain (as in the section before). Then, it follows a process called *pinching*, consisting in reducing the uncertainty of each input parameter to a baseline value, and comparing the uncertainty on the output before and after performing pinching for that parameter [19]. The score for each parameter k is calculated as:

$$Score_k = 1 - \frac{Distance(R_0)_k}{Distance(R_0)_{Total}} \quad (1)$$

where $Distance(R_0)_k$ is the width of the major radius output interval when uncertainty in parameter k has been reduced to a baseline point keeping all the other parameters uncertain, and $Distance(R_0)_{Total}$ is the width of the major radius output interval when all the input parameters are uncertain. The larger the score, the greater the impact of that parameter on the output uncertainty. It is important to note that this metric does not necessarily sum up to 1.

Lastly, data was classified in two categories: feasible and unfeasible. The dependence of the feasibility with the different parameters is visualised with density functions, aiding the identification of the parameter space regions with higher or lower density of feasible samples.

TABLE II
RESULTS OF MAJOR RADIUS UNCERTAINTY QUANTIFICATION.

Major Radius	metres
Minimum:	7.929
Maximum:	10.322
Distance:	2.393

IV. RESULTS

Results of the impact of parameters uncertainty on the major radius of the European H-mode DEMO baseline are summarised in Table II. The results suggest that, given the current state of the knowledge on the design parameters, the maximum length the baseline can deviate from the predictions is 2.393 metres.

The current estimation for the EU-DEMO baseline major radius is 9.0 metres [10], which is inside the predicted interval of [7.929,10.322] metres. However, values greater than 9.0 metres are also predicted considering design uncertainties, meaning that there is a possibility of EU-DEMO being larger than currently estimated.

Visualising the scatterplots, major radius showed strong dependence on the H-factor (Figure 1), plasma elongation (Figure 2), and thermal He-4 fraction (Figure 3), suggesting that for this analysis these are the parameters with highest impact on the major radius uncertainty inside PROCESS. When these parameters are uncertain, the operational divertor limit, core radius, and tungsten impurity fraction seem to have little impact on the major radius uncertainty.

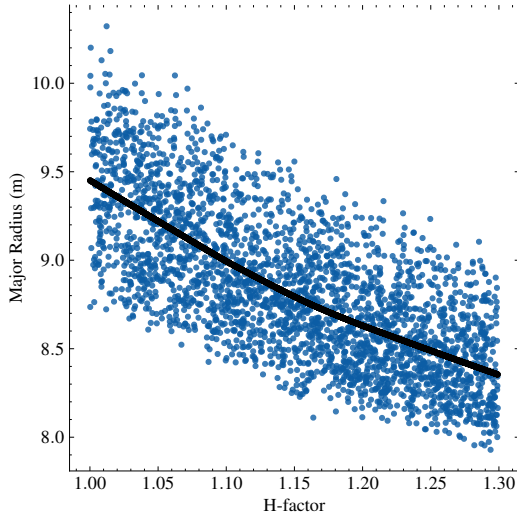


Fig. 1. Scatterplot of major radius against H-factor. Black line is a locally weighted linear regression to help with the trend visualisation.

The results suggested by the scatterplots are confirmed by the pinching sensitivity analysis, which results are summarised in Table III. Reducing thermal He-4 fraction uncertainty to its baseline point would reduce the major radius uncertainty 39.35%, whilst reducing divertor limit uncertainty would return a negligible reduction of 0.75%.

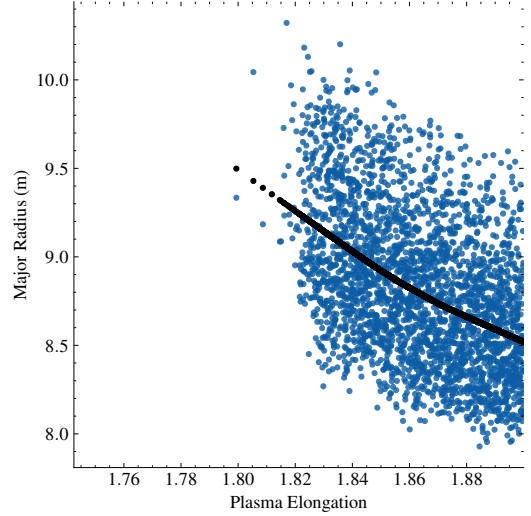


Fig. 2. Scatterplot of major radius against plasma elongation. The missing data for values of plasma elongation ≤ 1.80 is due to the fact that PROCESS was unable to find feasible solutions in that parameter space.

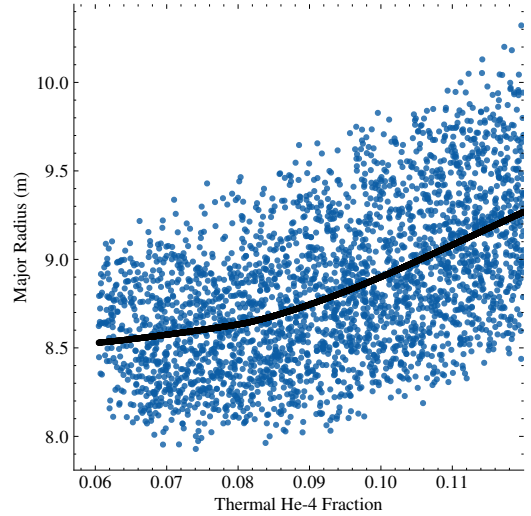


Fig. 3. Scatterplot of major radius against thermal He-4 fraction.

TABLE III
REDUCTION OF MAJOR RADIUS UNCERTAINTY AFTER PINCHING EACH CORRESPONDING PARAMETER TO ITS BASELINE VALUE. CALCULATED AS IN (1).

Parameter	Uncertainty Reduction
Thermal He-4 Fraction	0.3935
H-factor	0.2766
Plasma Elongation	0.1647
W Impurity Fraction	0.1130
Core Radius	0.0186
Divertor Limit	0.0075

Regarding feasibility, it showed highest dependence with the plasma elongation and the thermal He-4 fraction. Diagonal of Figure 4 indicates the density of samples that belong to each category (feasible or unfeasible). For the plasma elongation, it is possible to discern a clear division of feasibility regions when it is around 1.83. There is also an increase in the feasibility as the thermal He-4 fraction increases. These results could indicate that the plasma elongation should be of at least 1.83 to fulfill the net electric power output constraint of 400 MW, as it has been shown that greater fusion power are associated with larger elongations [6], and larger concentrations of thermal He-4 in the plasma are favourable to achieve the pulse length constraint of 2 hours, since it has been shown that He-4 contributes to increase the energy confinement time when it does not exceed the dilution upper limit [22].

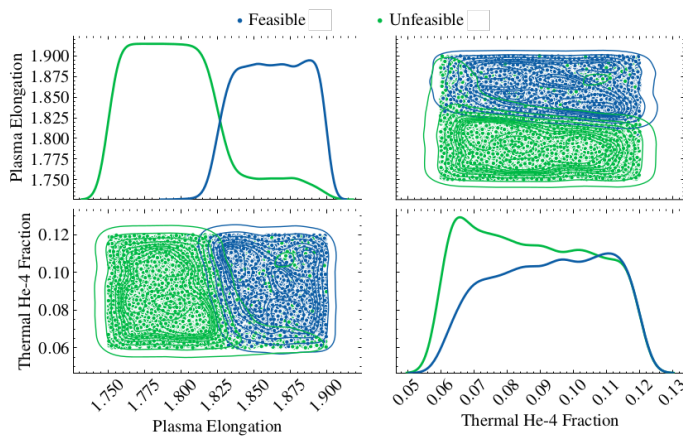


Fig. 4. Density plots (diagonal) and joint density plots of plasma elongation and thermal He-4 fraction data classified as feasible or unfeasible.

V. CONCLUSION

This is the first work on epistemic uncertainty propagation in the form of intervals using PROCESS. The objective was to develop the methodology and computational tools required to compare the impact of uncertainty on different DEMO concepts, and the European H-mode DEMO baseline served as use case. The resources developed for this work can be helpful to identify areas with significant impact on the uncertainty of fusion power plants, and provide information during DEMO concept design and selection.

In the case of the European H-mode DEMO baseline, we found that H-factor, plasma elongation, and thermal He-4 fraction had the largest impact on the uncertainty of the major radius as well as the PROCESS feasibility, given the parameter space explored.

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