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# Tomographic reconstruction of tokamak edge turbulence from single visible camera data and automatic turbulence structure tracking

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## Abstract

Following the lead of [Nguyen Van Yen Nucl. Fus. **52** (2012) 013005 (11pp)], this article tackles the problem of tomographic inversion with one camera assuming a constant emissivity of light along the magnetic field lines. In this way, the 3D problem reduces to 2D by helical symmetry, allowing for the reconstruction of any poloidal plane in the field of view of the camera. It is shown in this article that the complexity of using a wavelet basis for the reconstruction, as presented by Nguyen, is not necessary. The method is also validated by confronting it to 3D numerical data coming from the TOKAM3X code, for which the emissivity is slowly varying along the field lines (up to 20 %), showing the robustness of the reconstruction. The technique is then applied to real camera data recorded during a D-shaped ohmic plasma shot realized in the COMPASS tokamak. The method is experimentally validated by comparing reconstructed data from camera and ion saturation currents measured by Langmuir probes in the divertor region. Finally, it is shown that automatic detection and tracking of structures visible in the reconstructed poloidal plane enables unique investigations of edge plasma physics and opens wide perspectives for this method.

## 1 Introduction

Edge plasma turbulence in toroidal magnetic fusion devices plays a significant role on particle and energy confinement as well as on plasma-wall interactions [33, 25]. Several diagnostics can be used to study this region, which extends radially from the material wall of the device to the vicinity of the separatrix, like electrostatic probes, beam emission spectroscopy, visible imaging, reflectometry... However, the interpretation of turbulence measurements remains difficult. In particular, visible imaging measures light emission resulting from the interaction between the plasma and neutral particles. In most tokamaks and stellarators, turbulence imaging is based on the local injection of neutral gas to enhance visible light emission. This technique, called gas puff imaging (GPI), facilitates the visualization of turbulent structures by increasing the signal-to-noise ratio and by localizing measurements to a nearly 2D cross-section [34, 23, 24, 10]. GPI enables excellent space-time resolution of fluctuations, making it possible to investigate scales ranging from 0.1 mm to a few centimeters and from a few kHz to about 1 MHz, thus covering the essential parts of the fluctuation spectrum in the concerned region. However, GPI is not passive and causes perturbations to the plasma. These perturbations can be evidenced by other diagnostics, but their dependence on many parameters makes them rather difficult to evaluate [34, 27, 21].

In this paper, we focus on the use of passive turbulence imaging, i.e. without any gas puff. This technique is intrinsically non-perturbative, but it suffers mostly from two disadvantages. First, the collected visible light can be very weak compared to GPI, resulting in a lower signal-to-noise ratio. Second, measurements are not localized due to the line-of-sight integration over the emission sources. Low visible light conditions are still an issue, which is however getting less and less critical as modern fast cameras get more and more sensitive. It is also possible to handle the issue of line-of-sight integration by performing tomographic inversion, as it was done with various approaches on several toroidal devices [16, 9, 18, 31]. With appropriate processing, it is possible to extract useful information from plasma visible light emission. We present here tomographic inversion applied to experimental video data recorded on the COMPASS tokamak [20] without any help of gas puff. The method is first illustrated

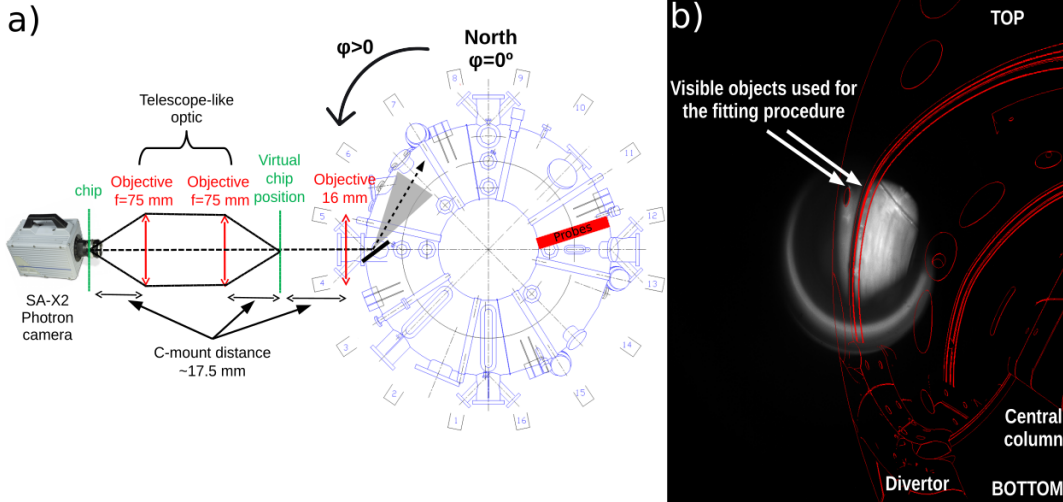


Figure 2.1: a) Schematic of the optical apparatus installed on COMPASS. The location of the probe array that will be used in Section 4.3 is also shown, as well as the convention taken for the angle  $\varphi$ . b) Rendering of the Calcam calibration on top of a calibration picture taken with the SA-X2 camera.

46 with an academic case and validated against simulation data of the 3D fluid turbulence code TOKAM3X. Then,  
 47 comparisons with probe measurements demonstrate its capability to reconstruct high-frequency fluctuations in any  
 48 2D plane intersecting the viewing volume. As we finally show, this makes it possible to analyze reconstructed data  
 49 statistically without any temporal averaging, providing high-resolution information of structure's dynamics.

## 50 2 Scrape-of-layer observation by fast visible camera on COMPASS

51 The scrape-of-layer (SOL) of the COMPASS tokamak was observed by a SA-X2 photron camera at a frame rate  
 52 of 270 kfps and an exposure time of about  $2.1 \mu s$ . At this speed, the resolution of the CMOS sensor is  $128 \times 144$   
 53 pixels, with each pixels having a  $20 \times 20 \mu m^2$  surface. Thanks to its high sensitivity (25 000 ISO) and dynamic range  
 54 (12-bits), the light fluctuation of the plasma edge was observed with no need for local gas injection (GPI), i.e. the  
 55 interaction between the neutral gas naturally present in the SOL and the plasma was enough to study the edge  
 56 turbulence.

57 The camera was placed at the 4/5 AL (angular lower, i.e. below the midplane) port of the device (see Fig. 2.1.a),  
 58 integrated to the rapid imaging system of COMPASS [15] and an aluminium mirror of  $22 \times 45 \text{ mm}^2$  was installed  
 59 in-vessel to collect the light coming from a zone centered around the last closed flux surface for D-shaped plasmas.  
 60 In addition, the mirror was tilted in such a way that the line of sights (LOS) were locally tangential to the magnetic  
 61 field lines at a distance of about 30 cm from the mirror location for the considered discharges. Therefore, a 16 mm  
 62 focal length objective was used with the camera and focused at about 30 cm. Because the camera is sensitive to  
 63 the magnetic field generated by the many coils surrounding the vessel, a telescope-like setup was used to put the  
 64 camera as far as possible from the stray magnetic field. This setup consists of two identical objectives of 75 mm  
 65 focal length placed in opposite directions and focused at infinity so that the rays in between the two objectives are  
 66 parallel to the optical axis providing that the rays comes from the focal plane of the first objective. Consequently,  
 67 the 16 mm objective creates an image in the focal plane of the first objective and the camera is located in the  
 68 one of the second objective. Therefore, the camera could be located at about 1 m from the vessel thanks to black  
 69 extension tubes in between the two 75 mm optics (see Fig. 2.1.a for a scheme of the optical apparatus). This optical  
 70 configuration allows a resolution of about 0.4 mm between two consecutive pixels at 28 cm from the mirror and  
 71 about 0.7-0.8 mm at 65 cm (i.e. at the vessel wall and slightly unfocused).

72 Performing tomographic reconstruction requires a precise localization of the camera and determination of the  
 73 field of view in the lab frame. On COMPASS, this calibration is done using the Calcam software [26] that compares  
 74 an image of the real field of view taken with the camera while enlightening the inside of the vessel and the CAD  
 75 representation of the machine. In this particular case, the field of view being very narrow and since very few features  
 76 on the vessel were visible, the CAD model was adjusted manually to fit as much as possible the calibration picture  
 77 (see Fig. 2.1.b).

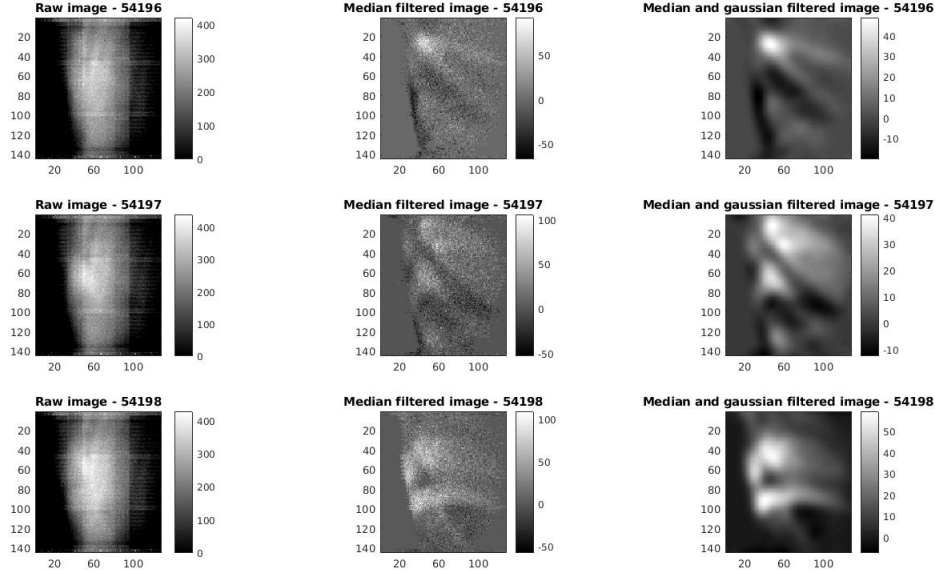


Figure 2.2: Left: three successive snapshots of the D shaped discharge #15487 taken at a sampling frequency of 270 kfps and an exposure time of  $2.1 \mu s$ . Middle: Images obtained after subtraction of a median image calculated over 10 frames around the considered picture. Right: Medianed filtered images after applying a spatial Gaussian filter with a standard deviation of 5 pixel.

78 As an illustration of how data look like, the left column of Fig. 2.2 shows three successive snapshots taken in  
 79 the D-shape plasma discharge #15487 during the flattop current plateau (discharge time  $\sim 1150$  ms). Since the  
 80 camera has a 12-bit dynamic, only the highest bits have been considered to display the images. One can notice  
 81 that structures are hardly distinguishable when looking at the raw data. In addition, stripes can be seen in both  
 82 horizontal and vertical directions. They are present there due to the different sensitivities of each sensor composing  
 83 the camera chip that was not corrected before recording the video. To reveal hidden structures, a sliding median  
 84 image calculated over 10 frames around the considered image has been subtracted from the raw data and is shown  
 85 in the central column of Fig. 2.2. Filamentary-like structures are then revealed, even though a non negligible noise  
 86 is present. The structures above the sliding median will be referred as positive structures while the one below the  
 87 median will be referred as negative. Note that the stripes due to the sensor sensitivity disappeared and did not affect  
 88 sensibly the fluctuating part of the signal. To further process the signal, a spatial Gaussian filter with a standard  
 89 deviation of 5 pixel was applied, smearing out structures below  $\sim 2$  mm. The noise is smeared out, the essential  
 90 part of the signal is retrieved but the filament dynamic stays complex for the human eye.

### 91 3 Tomographic reconstruction

92 Unlike gas-puff imaging experiments, the measurement presented in Fig. 2.2 is not located in a poloidal plane but  
 93 is the result of the integration of the light along each line-of-sight of the camera, i.e. the image is the projection  
 94 of a 3D structure onto the 2D camera chip. Therefore, information about the radial velocity or the perpendicular  
 95 blob dimension is not straightforwardly inferred. Years ago, a tomographic method has been proposed by Nguyen  
 96 Van Yen *et al.* [31] to recover the poloidal plane corresponding to circular edge plasma from camera data assuming  
 97 constant light emissivity of the turbulent structures along the magnetic field lines. Other techniques exist to perform  
 98 tomographic inversion in this case, such as the least-squares method or the singular value decomposition (SVD)  
 99 reconstruction, but it has been shown that they are both less efficient than the technique used in Ref. [31]. To  
 100 our knowledge, the method has not been used since then probably due to its rather complicated mathematical  
 101 development and the high signal to noise ratio that the method requires to observe and follow fast structure  
 102 movements without any additional light source than neutral atoms naturally present in the SOL of the tokamak.  
 103 However, cameras' sensitivity as well as their speed have improved significantly in the past years making the method  
 104 relevant to fusion plasma edge turbulence studies. Due to the complexity of the method presented in Ref. [31], we

105 recall in some details in this section the procedure that was used to recover fluctuation's structures in a 2D poloidal  
 106 cross-section from a 3D structure projected along the different lines of sight of the camera, assuming constant  
 107 emissivity along the magnetic field lines. We also show that the projection basis does not necessary have to be a  
 108 wavelet basis, simplifying the implementation of the method.

### 109 3.1 General principle

110 The camera apparatus is approximated by a screen collecting the light passing through a pinhole located at the  
 111 pupil of the camera objective. Let  $S_0(\psi, \theta, \varphi)$  be the plasma emissivity at a point  $M$  characterized by its fieldline  
 112 coordinates  $(\psi, \theta, \varphi)$ , where  $\psi$  is a flux coordinate,  $\theta$  a poloidal coordinate and  $\varphi$  the toroidal angle. Assuming that  
 113 radiations are isotropic, that the plasma is transparent and that radiations are mainly coming from  $H_\alpha$  and  $D_\alpha$   
 114 radiations so that the spectral response of the camera does not play a role, the intensity collected by the camera at  
 115 the pixel  $(x, y)$  is given by

$$I_0(x, y) = \int_{s_c}^{+\infty} S_0(\psi(s_{xy}), \theta(s_{xy}), \varphi(s_{xy})) ds_{xy} \quad (3.1)$$

116 where  $(x, y)$  are the horizontal and vertical coordinates in the image plane,  $s_{xy}$  is the curvilinear abscissa along  
 117 the ray passing through  $(x, y)$  and  $s_c$  the position of the camera pupil.

118 The goal of the tomographic inversion is to retrieve the local plasma emissivity  $S_0$  knowing the camera picture  
 119  $I_0$  by inverting Eq. 3.1. The structures that one is willing to recover being three dimensional and the image 2D,  
 120 it is therefore necessary to make one more assumption for the problem to be solvable. We thus assume that the  
 121 emissivity of the observed structures is constant, or slowly varying, along the magnetic fieldlines within the field  
 122 of view of the camera. This hypothesis is justified by the fact that the parallel velocity of the particles along the  
 123 fieldlines is high [29] and, in the particular case of this article, that the view is narrow (about  $\Delta\varphi = 75^\circ$  is visible  
 124 by the camera). Thanks to the helical symmetry of the fieldlines, the problem now reduces to recover the emissivity  
 125 in any 2D poloidal cross section  $S_0(\psi, \theta, \varphi_r)$ , located at the toroidal angle  $\varphi_r$ , knowing the 2D image  $I_0$ .

### 126 3.2 Transfer matrix creation

127 This poloidal cross-section located at the toroidal angle  $\varphi_r$  will be called in the following the reference poloidal  
 128 plane. It is in that plane that the emissivity pattern will be reconstructed from the camera image. In order to  
 129 handle the inversion numerically, the reference poloidal plane is discretized on a mesh grid, the image plane being  
 130 already discretized by the pixels of the CCD sensor of the camera. Thus, any cell of the meshgrid of the reference  
 131 poloidal plane ( $\varphi = \varphi_r$ ) is associated to a homogeneous structure inside the magnetic flux tube passing through  
 132 this cell.

133 Let us now consider the mapping  $\mathcal{K}$  that associates any emissivity pattern that can be built on the reference  
 134 plane mesh grid to the image on the camera of the related 3D emission structure, given by helical symmetry along  
 135 magnetic flux tubes. From Eq. 3.1, we know that  $\mathcal{K}$  is a linear mapping. Thanks to the discretization of the  
 136 reference poloidal plane, both the source set (the set of emissivity patterns in the reference plane) and the target set  
 137 (the set of all the possible images on the CCD camera) are of finite dimension. Thus Eq. 3.1 can be written in terms  
 138 of matrices, i.e., following the notation of Ref. [31],  $I_0 = K S_0$ , where  $S_0$  is the vector containing the emissivity of  
 139 each cell of the mesh grid of the reference poloidal plane,  $I_0$  the vector containing the intensity of each pixel of the  
 140 CCD camera and  $K$  is the matrix associated to the mapping  $\mathcal{K}$ .

141 Practically, we computed the transfer matrix  $K$  as follows:

- 142 • In order to avoid unnecessary calculation, we take into account the actual field of view of the camera. In  
 143 a poloidal plane, a point is characterized by  $R$ , its distance to the main axis of the torus and  $z$ , its height,  
 144 whose origin is the equatorial plane. We consider the path through the torus of the four extrem lines-of-sights  
 145 passing by the camera pupil and by one of the four pixel corners of the CCD sensor of the camera. We  
 146 compute the minimum radius  $R_{min}$  reached by the most inner LOS, the maximum radius  $R_{max}$  is taken as  
 147 the radius of the external wall in the equatorial plane, the minimum and the maximum height  $z_{min}$  and  $z_{max}$   
 148 are the minimum and the maximum height of these four LOS inside the torus.
- 149 • The reference poloidal plane is then chosen within the field of view of the camera. We usually choose the  
 150 reference plane to correspond to the focal plane of the camera.
- 151 • The reference poloidal plane is discretized on a cartesian mesh grid. Any mesh cell center  $G$  has coordinates  
 152  $(R_G, Z_G)$  such that  $R_{min} < R_G < R_{max}$  and  $z_{min} < Z_G < z_{max}$ .



- 153 • A look-up table is created, by integrating the magnetic lines passing by each mesh grid point using the  
154 magnetic topology calculated by the EFIT reconstruction software [3]. This makes it possible to associate  
155 any point inside the torus to the cell of the mesh grid of the reference poloidal plane that is magnetically  
156 connected to it (unless the point is not connected to any cell of the mesh grid).
- 157 • Numerical integration of Eq. 3.1 along each LOS to get the transfer matrix  $K$ . One LOS corresponds to one  
158 pixel on the CDD sensor whose coordinates in the sensor plane are  $(x, y)$ ,  $x$  and  $y$  being integer indexes. Let  
159  $M$  be a point on the LOS associated to the pixel  $(x, y)$ , at the center of an integration step. Let  $\Delta l$  be the  
160 length of the integration step of the numerical integration at point  $M$ . If  $M$  is magnetically connected to  
161 the cell  $(i, j)$  of the mesh grid of the reference poloidal plane, then  $K$  is incremented at the integration step  
162 centered on  $M$  as follows

$$K(x, y, i, j) = K(x, y, i, j) + \Delta l \quad (3.2)$$

163 As a result, for one given cell of indexes  $(i_0, j_0)$ ,  $K(x, y, i_0, j_0)$  is the image on the camera of the structure  
164 along the magnetic flux tube passing through this cell of index  $(i_0, j_0)$ , with an emissivity equal to one inside  
165 that magnetic flux tube and vanishing elsewhere (see Fig. 3.1 a) and b) for a practical example).

### 166 3.3 Matrix inversion

167 The method to calculate the elements of the transfer matrix  $K$  being presented, we are now discussing and explaining  
168 the method to invert it. Explanations are admittedly already available in Ref. [31], but we think it is worth giving  
169 some more details for a better understanding. Discussion is mainly about the invertibility of the mapping  $\mathcal{K}$ . What  
170 are the condition to fulfill for  $\mathcal{K}$  to be invertible? In Ref. [31], invertibility is merely assumed and it was only  
171 observed numerically that the matrix  $K$  was actually invertible in the case treated.

172 The strength of the method used in Ref. [31] is the way the matrix  $K$  is built, as explained in the previous  
173 subsection. The transfer matrix  $K$  yields the image on the camera screen of each magnetic flux tube whose cross-  
174 section in the reference poloidal plane is one cell of the cartesian mesh  $(i, j)$ . The ensemble of the images of those  
175 structures and all the linear combinaison of them is a subset of the ensemble of the images that can be drawn on  
176 the camera.

177 A first necessary condition for the mapping  $\mathcal{K}$  to be a one to one mapping (bijective), and thus invertible, is  
178 that this subset of the ensemble of the images is equal to the set of all images likely to be recorded during one shot  
179 by the camera as they are after the preprocessing described in Section 2. This implies that there is no structure  
180 smaller than the scale of the mesh grid and yet resolved by the camera. Notice that the gaussian filter that is  
181 applied to camera images, as explained in Section 2, not only removes noise but also removes or enlarges, if its  
182 width is properly choosen, such too small structures, that cannot be reproduced by a linear combination of the  
183 images of the mesh magnetic flux tubes (i.e. the magnetic flux tube passing through the different mesh cells). A  
184 great care should also be taken to the areas of the CCD sensor that collect no light due to obstacles between the  
185 plasma and the camera. They have to be discarded from the image grid.

186 Another necessary condition is to discard from the source set basis all the mesh cells in the reference poloidal  
187 plane whose corresponding flux tube are invisible on the camera.

188 The last necessary condition is that the size of the cell of the mesh grid of the reference plane is large enough  
189 so that their images can be resolved by the camera (i.e. two different cells yield two distinguishable images).

190 All those necessary conditions taken together seem to us sufficient to ensure that the mapping  $\mathcal{K}$  is a one to  
191 one mapping. Then it is worth inverting the transfer matrix  $K$ , as it will make possible to get the shape of the  
192 structure cross-section in the reference poloidal plane, at the resolution of the chosen mesh grid. Consequently, the  
193 inversion method will be now explained.

194 Let  $(\psi_\lambda)_{\lambda \in [1..N_\lambda]}$  be an orthogonal basis of the reference poloidal plane mesh, where  $N_\lambda$  is the number of nodes  
195 on the mesh in the reference poloidal plane whose image on the camera is non-zero. In such a basis, the light  
196 emissivity  $S_0$  can be written as

$$S_0 = \sum_{\lambda=1}^{N_\lambda} s_\lambda \psi_\lambda = \sum_{\lambda=1}^{N_\lambda} \langle \psi_\lambda | S_0 \rangle \psi_\lambda \quad (3.3)$$

197 where  $\langle . | . \rangle$  means dot product, both in the reference poloidal plane mesh grid and in the image plane. The image  
198  $I_0$  of  $S_0$  by  $\mathcal{K}$  reads

$$I_0 = K S_0 = \sum_{\lambda=1}^{N_\lambda} s_\lambda K \psi_\lambda, \quad (3.4)$$

199 where  $K \psi_\lambda$  is the matrix containing the intensity of each pixel related to the image on the camera of the basis  
 200 vector of the reference poloidal plane  $\psi_\lambda$ . As discussed in the previous paragraph, the mesh grid in the reference  
 201 poloidal plane and the Gaussian filter are chosen so that  $(K \psi_\lambda)_{\lambda \in [1..N_\lambda]}$  is a basis of the ensemble of all the possible  
 202 images that can be obtained from the camera after the preprocessing detailed in Section 2.

203 Then, it comes from Eq. 3.4 that if the decomposition of the preprocessed image on the basis  $(K \psi_\lambda)_{\lambda \in [1..N_\lambda]}$  is  
 204 found (i.e. the coefficients  $s_\lambda$ ), the related emissivity field in the reference plane is recovered. The only difficulty is  
 205 that the image by  $K$  of the basis  $(\psi_\lambda)_{\lambda \in [1..N_\lambda]}$  is not orthogonal. Thus to get the coefficients  $s_\lambda$ , the adjoint basis  
 206 of  $(K \psi_\lambda)_{\lambda \in [1..N_\lambda]}$  have to be processed.

207 Let  $\mathcal{P}$  be the set of the structures on the reference poloidal mesh grid, reduced to the nodes whose image on the  
 208 camera is non vanishing, and let be  $\mathcal{I}$  the ensemble of the images on the areas of the CCD sensor illuminated by  
 209 the plasma. Then, the adjoint basis is related to the adjoint operator  $K^*$ , defined as follows

$$\forall (a, b) \in \mathcal{P} \times \mathcal{I}, \langle Ka|b \rangle = \langle a|K^*b \rangle \quad (3.5)$$

210 Note that  $K$  is defined on  $\mathcal{P}$  whereas  $K^*$  is defined on  $\mathcal{I}$ .

211 Now considering the  $N_\lambda$  vectors of the orthonormal basis of  $\mathcal{P}$  called  $(\psi_\lambda)_{\lambda \in [1..N_\lambda]}$ , as  $K$  is invertible (and thus  
 212  $K^*$ ), there exist two corresponding image families  $(\chi_\lambda)_{\lambda \in [1..N_\lambda]}$  and  $(\xi_\lambda)_{\lambda \in [1..N_\lambda]}$ , both in the image plane  $\mathcal{I}$  defined  
 213 by

$$\begin{aligned} K \psi_\lambda &= \kappa_\lambda \chi_\lambda \\ K^* \xi_\lambda &= \kappa_\lambda \psi_\lambda \end{aligned} \quad (3.6)$$

214 where  $\kappa_\lambda$  is chosen in order to impose  $\|\xi_\lambda\| = 1$  for all  $\lambda$  (useful condition to apply the thresholding method  
 215 described in the next section) and where  $\|\cdot\|$  is the norm in both  $\mathcal{P}$  and  $\mathcal{I}$ . The matrix  $K$  being invertible, those  
 216 two families are two bases of the set  $\mathcal{I}$  and  $(\xi_\lambda)_{\lambda \in [1..N_\lambda]}$  corresponds to the adjoint basis that we are looking for.  
 217 The equation that gives the reconstructed emissivity in the reference poloidal plane  $S_0$  can now easily be found  
 218 from Eqs. 3.3, 3.5 and 3.6 and reads

$$S_0 = \sum_{\lambda=1}^{N_\lambda} \langle I_0 | \xi_\lambda \rangle \kappa_\lambda^{-1} \psi_\lambda \quad (3.7)$$

219 From Eq. 3.3 and 3.7, it comes that the coefficients of the  $\psi_\lambda$  of the stucture in the reference poloidal plane read

$$s_\lambda = \langle I_0 | \xi_\lambda \rangle \kappa_\lambda^{-1} \quad (3.8)$$

220 In the following, we call  $s_{\xi_\lambda}$  the dot product of the image on the camera by the adjoint basis vector  $\xi_\lambda$

$$s_{\xi_\lambda} = \langle I_0 | \xi_\lambda \rangle \quad (3.9)$$

221 The last step that needs to be done is to find the  $N_\lambda$  coordinates of the elements of the  $\xi_\lambda$  basis, which is done  
 222 by solving a  $N_\lambda$  number of  $N_\lambda \times N_\lambda$  linear systems obtained using the biorthogonality condition that results from  
 223 Eqs. 3.5 and 3.6, i.e.

$$\langle \xi_\lambda | \chi_{\lambda'} \rangle = \begin{cases} 1 & \text{if } \lambda = \lambda' \\ 0 & \text{otherwise} \end{cases} \quad (3.10)$$

### 224 3.4 Basis choice and denoising

225 To apply the method describe above, it is then necessary to choose an orthogonal basis  $(\psi_\lambda)_{\lambda \in [1..N_\lambda]}$  of the discrete  
 226 reference poloidal plane. From the above demonstration, it is clear that the method does not require the basis  
 227 of the discretized reference poloidal plane to be of any particular form for the inversion method to be correct. It  
 228 just has to be orthogonal. For simplicity, we have chosen base vectors that correspond to each grid nodes of the  
 229 reference poloidal plane that yields a non vanishing image on the camera CCD sensor with an emissivity equals to  
 230 one, as they define an orthonormal base. An example of a  $\psi_\lambda$  vector is represented in Fig. 3.1 as well as the  $\chi_\lambda$  and  
 231  $\xi_\lambda$  families obtained from Eq. 3.6.

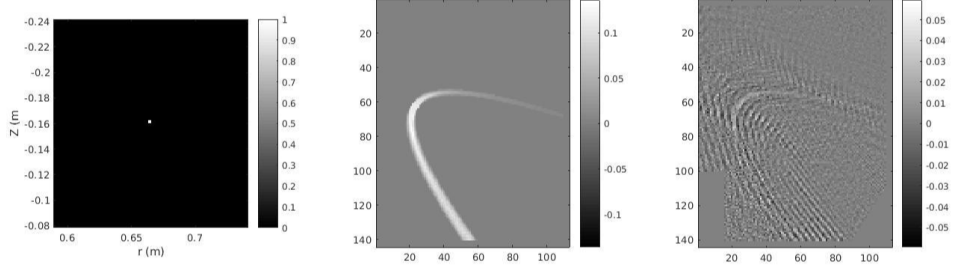


Figure 3.1: One example of a base vector  $\psi_\lambda$  (a single grid node) in the reference poloidal plane (left) and of the corresponding  $\chi_\lambda$  (middle) and  $\xi_\lambda$  (right) families in the image plane.

232 Note that in Ref. [31] the method was applied to a basis of wavelet vectors, used mainly for denoising purpose  
 233 (wavelet-vaguelette decomposition). Regarding the additional complexity brought by the use of wavelet theory, we  
 234 have chosen a simpler basis and we will show in the next sections that the final results are good enough so that  
 235 the use of wavelets, even for denoising, is not a must in our case. We used the same denoising technique as the one  
 236 proposed in Ref. [31], that eliminates all coefficients  $s_{\xi_\lambda} = \langle I_0 | \xi_\lambda \rangle$  in Eq. 3.7 below a threshold  $\Theta$  calculated from  
 237 the data themselves. It is for this thresholding technique that the dual basis has to be normalized, otherwise the  
 238 coefficients associated with the  $\xi_\lambda$  with the smallest norms would be artificially large. The threshold is the limit of  
 239 a sequence whose initial term is

$$\Theta_0 = \frac{c^2}{N_\lambda} \sum_{\lambda=1}^{N_\lambda} s_{\xi_\lambda}^2 \quad (3.11)$$

240 where  $c$  is a dimensionless constant close to unity which control the denoising sensitivity. At stage  $n$  all the  
 241 coefficients  $s_{\xi_\lambda}$  whose absolute value is lower than  $\Theta_n$  are discarded from Eq. 3.11 to calculate the next term of the  
 242 sequence, that eventually converges to a limit. The  $n + 1$  term reads

$$\Theta_{n+1} = \frac{c^2}{N_n} \sum_{\lambda/|s_{\xi_\lambda}| \geq \Theta_n}^{N_n} s_{\xi_\lambda}^2 \quad (3.12)$$

243 where  $N_n$  is the number of coefficients  $s_{\xi_\lambda}$  larger or equal to  $\Theta_n$ . More details can be found in the Refs. [31, 4].

244 Last, the typical calculation time on a standard computer and without any optimisation of the algorithm for  
 245 a  $64 \times 64$  mesh grid in the reference poloidal plane is about 5 minutes for the calculation of the look-up table, two  
 246 hours for the calculation of the transfer matrix  $K$  and its inversion, and then five seconds per image (assuming that  
 247 the magnetic field is constant over the extract of the movie processed) to obtain the reference poloidal plane after  
 248 denoising, i.e. about fourteen hours for a 10 000 image movie.

## 249 4 Validation

250 Sources of possible errors in such a tomographic reconstruction are numerous: errors in the code, mathematical  
 251 typos, wrong assumptions (especially assuming a constant emissivity along the field lines), noise amplification,  
 252 non-inversability of the  $K$  matrix. We propose in this section three different validation levels of the method. First,  
 253 we will show that there are no mathematical or code errors in the program by reconstructing an academic case,  
 254 with additional noise to further check the thresholding method. Second, taking a more relevant configuration from  
 255 a TOKAM3X simulation [28], we will show that the reconstruction is valid even in the case of a slowly varying  
 256 emissivity along the magnetic field lines. Third, the reconstruction will be applied to real data obtained on the  
 257 COMPASS tokamak and will be compared to probe data to validate the method under experimental conditions.

### 258 4.1 Academic case

259 At first, the whole procedure needs to be checked by simple test cases. We therefore consider the simple case of  
 260 a single node structure in the mesh grid of the reference poloidal plane, as shown in Fig. 3.1 (left). The synthetic  
 261 image seen by the camera is given by the central picture in Fig. 3.1. To test the thresholding method proposed in  
 262 Ref. [31], we add a strong white noise (having random values in between  $\pm 32\%$  of the maximum pixel intensity

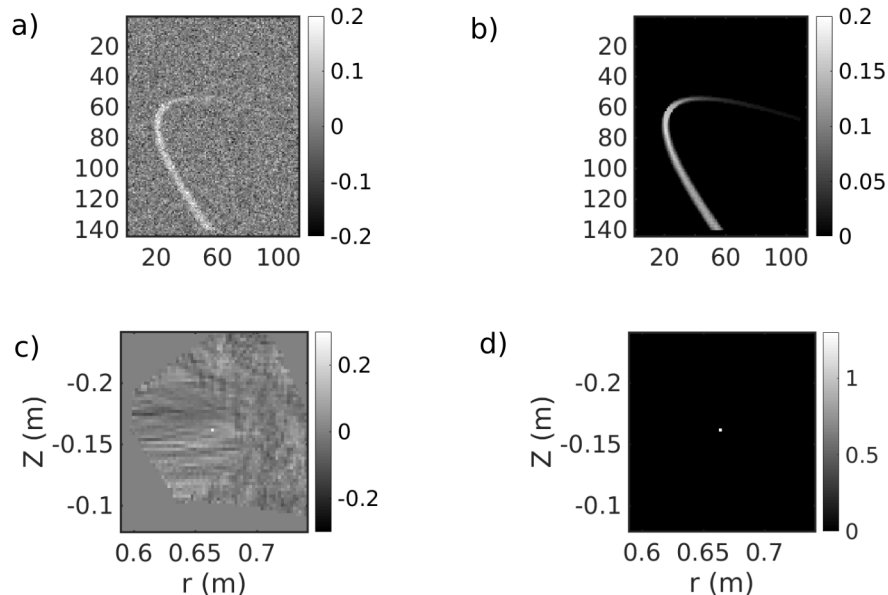


Figure 4.1: a) Noisy image generated after Fig. 3.1. b) Reconstructed image by applying  $KS_{rec}$ . c) Reconstructed poloidal plane  $S_{threshold}$  and d)  $S_{rec}$ . Figure d) is obtained after thresholding  $S_{threshold}$  with  $c = 3.5$ .

263 of the total image) to the picture and obtain Fig. 4.1 (a). We then apply the tomographic reconstruction described  
 264 in the previous section and present two images (Fig. 4.1 (c) and (d)). Fig. 4.1 (c) represents the coefficients  $s_{\xi_\lambda}$   
 265 associated to each node of the poloidal plane (see Eq. 3.9) that will be called  $S_{threshold}$  in the following sections.  
 266 This image serves to understand how the thresholding method works and shows that, even without projecting on a  
 267 wavelet basis, the coefficient corresponding to the relevant signal is well above the ones corresponding to the white  
 268 noise. Applying the threshold procedure with the parameter  $c$  being set to 3.5, the coefficients  $s_\lambda$  (see Eq. 3.7 and  
 269 3.8) associated to each node of the poloidal plane are plotted in Fig. 4.1 (d), that we will be called  $S_{rec}$  in the  
 270 following. One can see that this image corresponds to the reconstructed structures in the reference plane taken at  
 271 the beginning of the procedure (Fig. 3.1, left). The value of the single point node after tomographic reconstruction is  
 272 equal to 1.3 whereas it was set to 1 initially, implying that the white noise added a 30% error on the intensity value  
 273 reconstruction. In addition, the reconstructed image in Fig. 4.1 (b) obtained after applying  $K$  to the reconstructed  
 274 poloidal plane shows how similar the picture is to Fig. 3.1 (middle), except from the slightly higher intensity level.  
 275 This whole procedure validates the mathematical background and code and shows that even under strong noise  
 276 corruption, the procedure can reveal the structure of the relevant signal.

## 277 4.2 Reconstruction apply to TOKAM3X data

278 We now take a case closer to experimental data by considering 3D data generated from the TOKAM3X code [28]. In  
 279 particular, we consider a virtual camera able to record a signal proportional to the electron density generated by the  
 280 code. It is interesting to point out that the density from the 3D data is not constant along the field lines within the  
 281 field-of-view of the virtual camera and varies within the 20% range, so that the reconstruction will show how robust  
 282 the method is in case of structures with an emissivity varying along the magnetic field lines. In Fig. 4.2 (a) and  
 283 (b), we show the poloidal plane  $S_{ref}$  of the density fluctuations taken as the reference plane and the corresponding  
 284 image on the camera obtained by computing  $I_0 = KS_{ref}$ , using the 3D data output from the code. Notice the high  
 285 spatial resolution that the TOKAM3X code produces. We then apply the tomographic reconstruction to the image  
 286  $I_0$  and obtain the reconstructed plane  $S_{rec}$  ( $s_\lambda$  coefficients from Eq. 3.8) in Fig. 4.2 (c) thresholded using  $c = 2$ .  
 287 For comparison, we show the interpolation of  $S_{ref}$  over the same grid as  $S_{rec}$  in Fig. 4.2 (d). In Fig. 4.2 (e), the  
 288 reconstructed image  $I_{rec} = KS_{rec}$  is shown for comparison with  $I_0$ . It can be stated that the reconstruction is able to  
 289 recover the important features of the main poloidal plane. In addition, even though the resolution of reconstruction  
 290 is lower (32x64) than the one from the TOKAM3X code, the two pictures in Fig. 4.2 (b) and (e) resembles quite  
 291 well, showing that the most important parts of the signal have been extracted. The method thus seems reliable  
 292 even in the more realistic case of structures extended along the field lines with slowly varying emissivity.

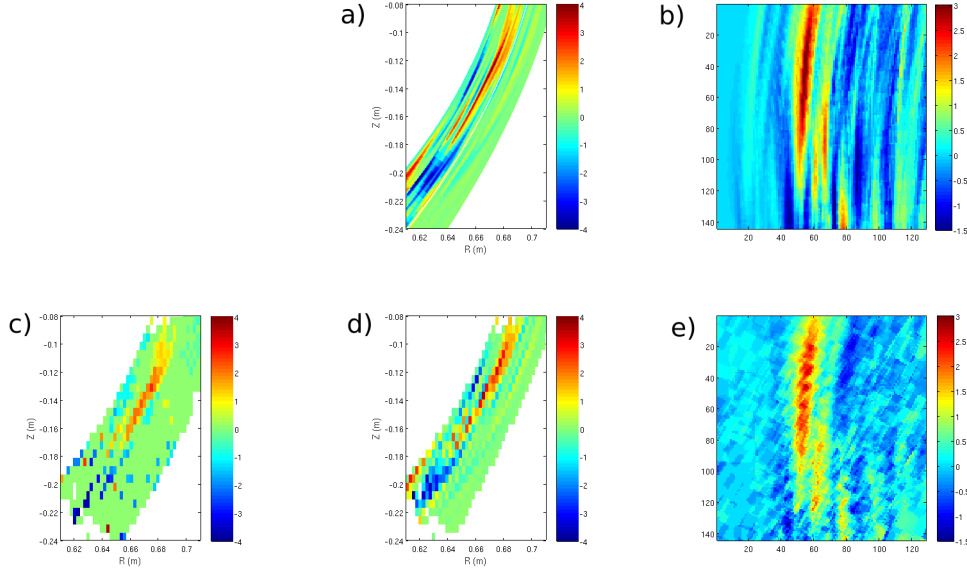


Figure 4.2: Tomographic reconstruction validation with TOKAM3X data. (a) Poloidal plane of reference  $S_{\text{ref}}$  obtained from the TOKAM3X code, (b) synthetic image obtained after applying  $I_0 = K S_{\text{ref}}$ , (c) reconstructed poloidal plane  $S_{\text{rec}}$  using  $c = 2$ , (d) interpolation of  $S_{\text{ref}}$  over the same grid as  $S_{\text{rec}}$ , (e) reconstructed image obtained by  $I_{\text{rec}} = K S_{\text{rec}}$ .

### 293 4.3 Real data: validation with probes

294 We now apply the reconstruction method to real data obtained in the COMPASS tokamak under the experimental  
 295 configuration presented in the first section. The data we present were measured during the discharge #15487 that  
 296 was a D-shape ohmic L-mode plasma with a main electron density of  $3 - 4 \times 10^{19} \text{m}^{-3}$ , a toroidal magnetic field of  
 297  $-1.15 \text{ T}$  and a plasma current of  $180 \text{ kA}$ . In that case (negative magnetic field and positive plasma current) and in  
 298 the LFS of the machine, the fieldlines are going down when rotating in the anticlockwise direction (for  $\varphi$  increasing  
 299 in Fig. 2.1). In order to compare the video data and probe data, we reconstructed 10 000 frames that correspond  
 300 to about 37 ms. The time of the first image corresponds to  $\sim 1137 \text{ ms}$ , selected in the middle of the flattop phase  
 301 of the discharge (phase about 180 ms long). For each image of the 10 000 frame video, a sliding median image  
 302 calculated over 10 frames was subtracted and a Gaussian filter with a standard deviation of 5 pixels was applied,  
 303 as already evoked in Section 2. In addition, camera pictures were shrunk to remove pixels for which no plasma was  
 304 visible, either because the port edge, where the mirror is inserted, is in the way or either because the mirror was not  
 305 big enough to cover the whole field of view of the camera. The poloidal plane that one is willing to reconstruct can  
 306 be any plane of the torus (provided that the assumption of constant emissivity holds until that plane). Here, we  
 307 have chosen the plane at toroidal angle  $\varphi = 55$  degrees, i.e. the focal plane of the camera. The reconstructed plane  
 308 was discretized by a cartesian grid of  $(R, Z) = (64, 64)$  cells, giving a spatial resolution of 2.4 mm in the horizontal  
 309 direction and 2.5 mm in the vertical one.

### 310 Snapshot example

311 In Fig. 4.3, we show a reconstruction example performed for the frame 54200 (time=1150.74 ms) of the selected time  
 312 period. The camera data after the median and the Gaussian filtering are shown in Fig. 4.3 (a), while Fig. 4.3 (b)  
 313 shows the reconstructed plane  $S_{\text{threshold}}$  (coefficients  $s_{\xi\lambda}$  in Eqs. 3.7 and 3.9) and Fig. 4.3 (c) shows the coefficients  
 314  $s_{\lambda}$  after the thresholding method was applied with  $c = 3.5$  (the denoised reconstructed structure in the reference  
 315 poloidal plane  $S_{\text{rec}}$ ). In both figures, the red line corresponds to the last closed flux surface from the EFIT  
 316 reconstruction software for that particular discharge time. The last image, Fig. 4.3 (d), shows the calculated image  
 317 in the camera plane  $I_{\text{rec}} = K S_{\text{rec}}$  obtained by applying the transfert matrix to the reconstructed structure  $S_{\text{rec}}$ .  
 318 One can note that the reconstructed image  $I_{\text{rec}}$  resembles well to the original one. In addition, on  $I_{\text{rec}}$  a zero value  
 319 rectangle is visible in the bottom left part of the image that corresponds to one edge of the mirror. Remember from  
 320 Section 3.3 that the line-of-sights collecting no light from the plasma should be discarded, for  $K$  to be invertible. A

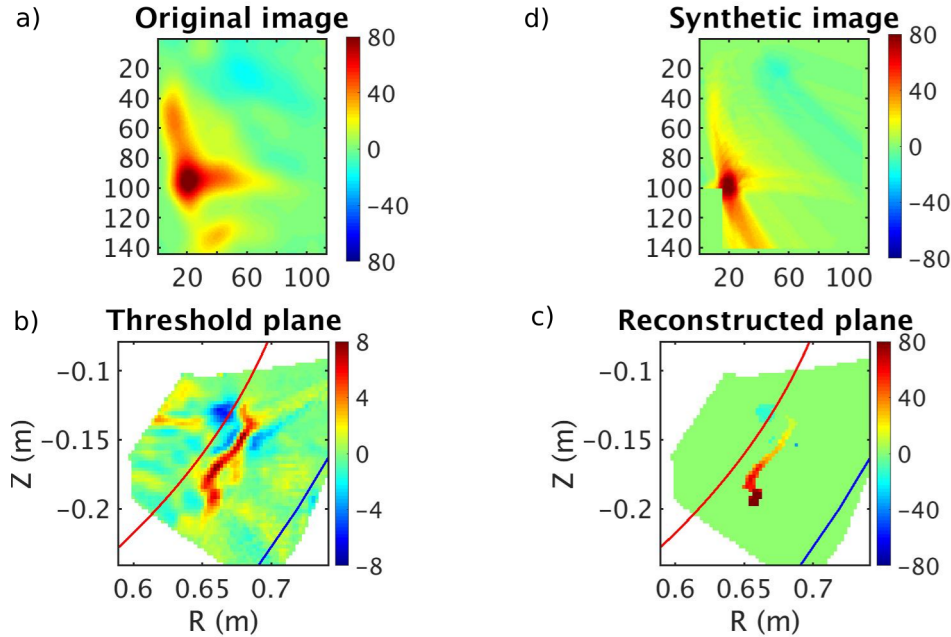


Figure 4.3: Tomographic reconstruction example for a snapshot taken at 1150.74 ms (frame 54200) of discharge #15487. (a) Camera data subtracted from a sliding median taken over 10 frames around the considered image and for which a Gaussian filter with a standard deviation of 5 pixels was applied, (b) reconstructed poloidal plane  $S_{\text{threshold}}$ , (c) reconstructed poloidal plane  $S_{\text{rec}}$  obtained applying the threshold method with  $c = 3.5$ , (d) reconstructed camera image from  $I_{\text{rec}} = K S_{\text{rec}}$ . The red line in figures (b) and (c) is the position of last closed flux surface given by the EFIT reconstruction while the blue line is the vessel wall position.

321 positive elongated structure is dominant on the reconstructed plane in Fig. 4.3 (c) but three negative structures (1  
 322 big and 2 small) are also visible, above the thresholding level and therefore relevant. It is also interesting to notice  
 323 that the intensity of the elongated positive structure varies from its top edge to its bottom edge. This aspect will  
 324 be commented in Section 5.

### 325 Validation with probes

326 To further convince the reader that the tomographic reconstruction extracts the important part of the data on  
 327 more than one snapshot, we have compared the reconstructed data with signals coming from Langmuir probes.  
 328 The divertor of COMPASS was recently equipped [1] with a 54 Langmuir probe array measuring ion saturation  
 329 currents (-270 V applied to the probes) located at  $\varphi = 127.5$  degree from the reconstructed plane. At that location,  
 330 mainly two probes are magnetically connected to the part of the reference poloidal plane visible in the camera field,  
 331 so-called LPA46 and LPA47 in the COMPASS database. In Fig. 4.4 (left column), the maximum of correlation of  
 332 the signal coming from these two probes and each pixel of the poloidal plane is presented. In addition, we show  
 333 for comparison the correlation of the camera data with the probe LPA39 which is not magnetically connected to  
 334 the visible part of the reference plane. In Fig. 4.4 (right column), the delay associated to the correlation is given in  
 335 microseconds, where a negative time delay means that the structure first reaches the probe before the reconstructed  
 336 poloidal plane. Note that the probe signals were interpolated (downsampled) to match the time window and step  
 337 of the 10 000 frames considered for the analysis. The magnetic fieldline connected to the probe is also represented  
 338 as a dashed red line and its ending point in the reference plane ( $\varphi = 55$  degrees) is shown as a red circle.

339 First, it is very interesting to see that the spatial maximum of correlation for the probe LPA47 is close to 0.4,  
 340 which is a strong value for two diagnostics measuring different physical quantities and magnetically separated by  
 341 about 2.4 m. Note that high correlation values were already observed on the TJ-K stellarator (see Fig. 4 of Ref. [11]  
 342 for instance) or on the Caltech tokamak [32], while on the Alcator C-Mod the maximum value was a bit lower (up  
 343 to 0.3) [14]. On linear devices, correlation values up to 0.5 can often be observed for direct comparisons [19, 2].  
 344 These high values are linked to the dependency of both signal with the electron density but modelling of the light  
 345 dependency with plasma parameters is out of the scope of this article. The spatial maximum value for the probe  
 346 LPA46 is lower (about 0.28) because the probe is magnetically connected to an area of the reconstructed plane for

347 which less signal is present. The signal to noise ratio is thus lower. On the other hand, the LPA39 probe that is  
348 not on any fieldline passing by the visible part of the reference poloidal plane has a weaker maximum of correlation,  
349 less than 0.13. It is important to add that the correlation between two consecutive probes on the divertor is very  
350 strong (for instance higher than 0.7 between probe LPA46 and LPA47) but also non negligible between more distant  
351 probes (for instance almost 0.25 between LPA39 and LPA47). This probably explains why, even though weak, the  
352 probe LPA39 does not have a zero correlation value.

353 Second, the spatial maximum of correlation for the LPA47 probe is close to the point magnetically connected to  
354 the probe and the region of maximum correlation is very similar in size and shape to the reconstructed structures  
355 (see Figs. 4.3 and 5.1). On the other hand, for the LPA46 probe, there are two spatial maxima, one close to the  
356 point magnetically connected to the probe and one above. This is first due to the fact that coherent structures  
357 travel poloidally on the reconstructed plane, and second, because most of the signal of the 2D plane comes from a  
358 region above the point magnetically connected to the probe.

359 Third, when looking at the delay figures, one sees that for the LPA46 and 47 probes, the region corresponding  
360 to non negligible correlation values depicts a color gradient, meaning that the time delay is evolving gradually  
361 from top (lower delay) to bottom (higher delay), and that structures are moving from top to bottom. This main  
362 average movement is visible by eyes when looking at the filtered camera data and is thus consistent with qualitative  
363 observations. It is also important to note that the time delay value near the points magnetically connected to both  
364 probes is identical (between  $-33$  and  $-36.7\mu s$  with  $3.7\mu s$  being the temporal resolution of the camera), even though  
365 the two points are at different poloidal location. Since the two probes are magnetically separated by about the same  
366 distance to the reconstructed plane (2.4 m), it is logical that the time delay is the same and it further validates the  
367 tomography reconstruction as different points in the 2D plane correspond to their conjugate on the divertor target.  
368 As a consequence, we consider from this last experimental checking and the ones in the two previous sections that  
369 the reconstruction method is valid and reliable.

## 370 5 First investigation of the properties of the reconstructed fluctuations

371  
372 The tomographic reconstruction of plasma fluctuations from single camera data offers interesting perspectives.  
373 First, the visualization of the structures in a poloidal plane enables direct comparison with simulation data [28].  
374 Second, a parallel objective is to ease the automatic processing of the videos in order to carry out the analysis  
375 of full length videos instead of focusing on some short sequences of interest. Ordinary, such sequences aim at  
376 illustrating rather basic aspects of a given phenomenon. As a result, one of the main criteria for selecting sequences  
377 of interest is the simplicity for the reader to understand the sequence which is depicted. It is however usually unclear  
378 whether the sequence is representative of the turbulence properties in the whole video and there is a significant  
379 risk to oversimplify the overall picture of the physics behind. It would be therefore of great interest to analyze  
380 complete shot videos under various discharge conditions in order to assess whether such sequences are statistically  
381 representative of the turbulence properties or not.

382 For such a reason, the TRACK software [5] has been chosen to analyze videos of reconstructed data. TRACK  
383 has evolved from the TRACE code already used in fusion research for investigations of plasma-wall interactions [6].  
384 The detection is based on auto-adaptive thresholding techniques which enable an efficient automatic detection  
385 in various conditions met in our experiments, while the tracking is based on predictive Bayesian methods. The  
386 comparison of automatic analysis results with manual tracking of the plasma structures in 3000 frames shows only  
387 minor differences, concentrated on sequences where the coexistence of several close structures does not give any  
388 certainty about the correct trajectories. The comparison of manual and automatic tracking for structures followed  
389 on 5 or more consecutive frames show no difference. In the following, we present some of the first results obtained  
390 with this approach, that shows the potential of the tomographic inversion coupled with a powerful detecting and  
391 tracking software.

### 392 Illustrative sequence

393 In Fig. 5.1, we present 10 successive reconstructed poloidal planes located at  $\varphi = 55$  degrees and measured during  
394 the discharge #15487. From frame 54195 (time  $\sim 1150.72$  ms) to frame 54204 ( $\sim 1150.76$  ms), one can see the  
395 appearance of a positive structure that moves poloidally and radially, before getting elongated in the poloidal  
396 direction and disappearing at some radial position. Starting from frame 54200, a negative structure appears and  
397 experiences a similar movement. In particular, the radial position where the structures get elongated and disappear  
398 is almost the same for both structures. This is a first hint on where the shear flow layer could be for that particular

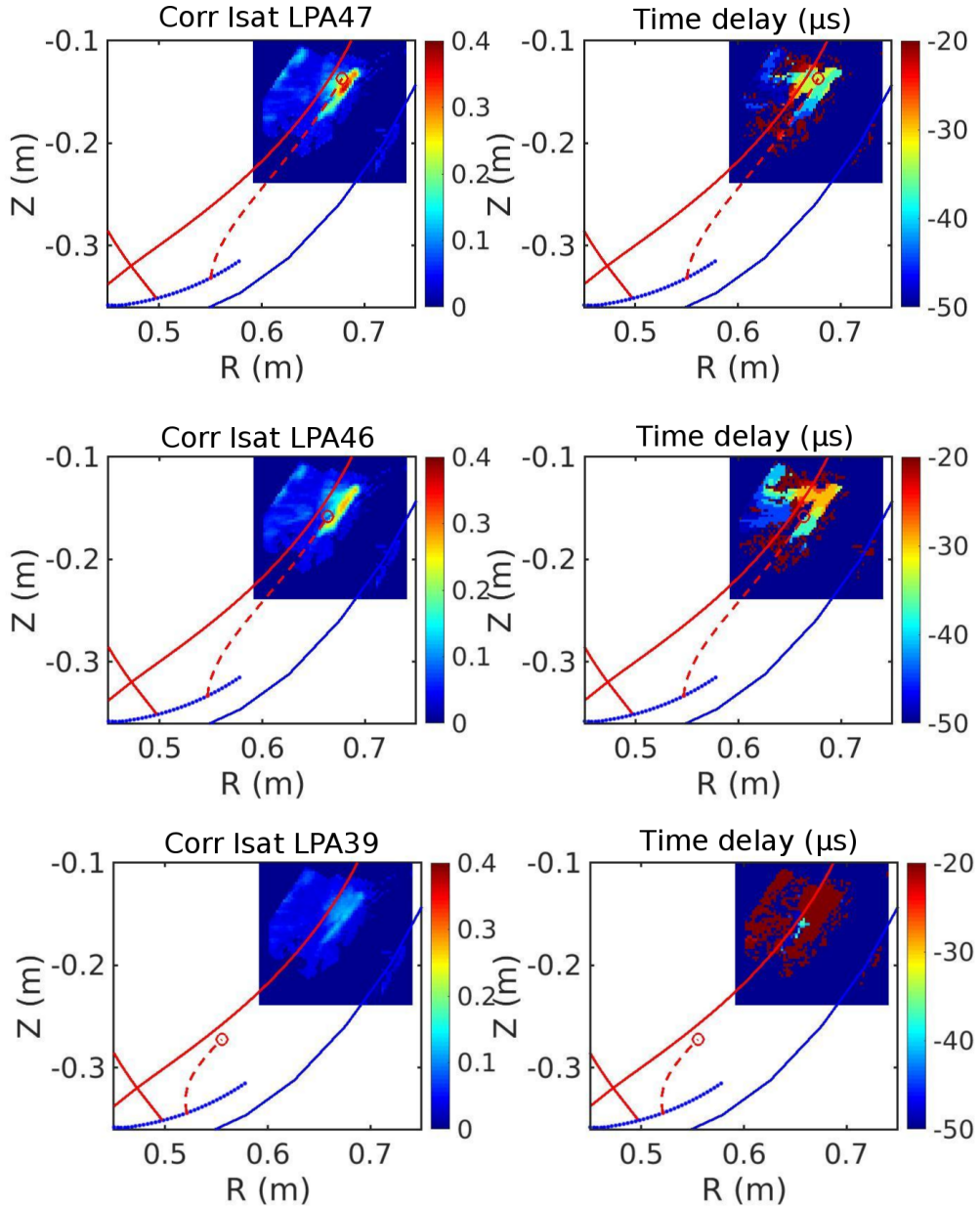


Figure 4.4: Maximum of correlation and associated delay between the ion saturation current measured by probes and the reconstructed camera data. Left column: normalized correlation value, right column: associated time delay in microseconds. Correlation for LPA47 (top), LPA46 (middle) and LPA39 (bottom). The red line represents the separatrix, the blue line, the vessel, and the dashed red line the magnetic fieldline starting from the probe position and finishing in the reconstructed plane (here  $\varphi = 55$  degree), as denoted by the red circle.



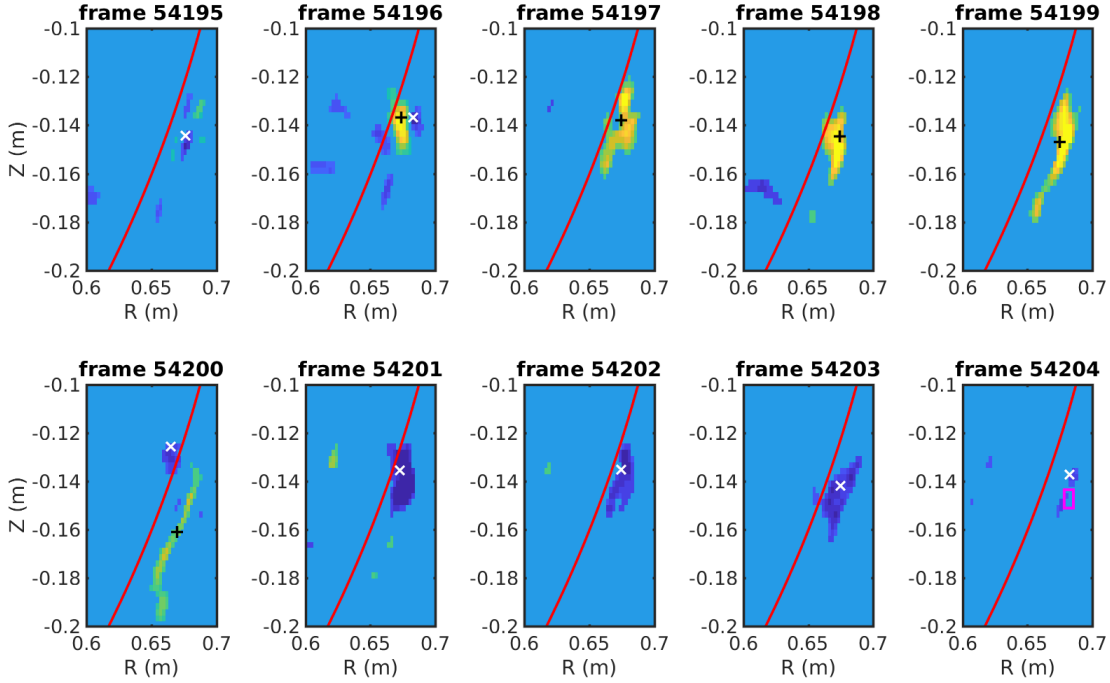


Figure 5.1: Reconstructed poloidal planes at  $\varphi = 55$  degrees for 10 frames taken from the discharge #15487 around  $\sim 1150$  ms. The thresholding method was applied with  $c = 3.5$ . The black (+) and white (x) crosses indicate the centre of mass of positive and negative structures, respectively, automatically detected and tracked by the TRACK software. The red line indicates the position of the separatrix from EFIT reconstruction. The pink rectangle corresponds to the zone chosen to obtain Fig. 5.2.

399 shot, about 1.5 cm outside from the separatrix calculated by the EFIT code. These structures are automatically  
 400 tracked with TRACK over 5 frames (18.5  $\mu$ s). For the positive structure, the total displacement is about 3.9 mm  
 401 in the radial direction and 22.6 mm in the poloidal direction, with a maximum perpendicular velocity of 900 m/s  
 402 and a maximum tangential velocity of nearly 3.5 km/s in the last part of the trajectory. Note that, we refer to  
 403 perpendicular velocities for velocity components locally perpendicular to the magnetic surfaces, while we refer to  
 404 tangential for velocities tangential to these surfaces.

405 We now come back to the observation we made in the previous section about the elongated structure visible in  
 406 the frame 54200. It is clear from the previous and next frames that the structure experiences a very fast movement  
 407 as it probably reaches a shear flow layer. This most likely explains why the structure in frame 54200 shows an  
 408 intensity gradient: during the recording time of the camera, it moves very fast downwards tangentially and at some  
 409 moment moves away perpendicularly. The whole movement happens in a very short time, probably shorter than  
 410 the exposure time of the camera that is only 2.1  $\mu$ s. It indicates that the camera was not yet recording fast enough  
 411 to fully resolve the dynamic near the shear flow region and should be set at least twice faster.

## 412 Evidence for complex turbulent dynamic

413 In order to go beyond the exploration of a short sequence, a full video composed of 10 000 frames (37 ms) has  
 414 been analyzed with the TRACK software (the same video sequence as used in Section 4.3). In total, 3637 positive  
 415 structures and 3811 negative structures have been automatically detected and tracked and the code main outputs  
 416 are their velocity, size, orientation and aspect ratio. Here, we will only present an example of what the velocity  
 417 distribution functions can be. A more sophisticated analysis will be presented in a separate paper.

418 For this analysis, we only consider the 626 positive structures that can be tracked on at least 5 consecutive  
 419 frames. In Fig. 5.2, we present the perpendicular and tangential velocity distributions obtained for these structures  
 420 and from a small rectangular region of 7.2 x 7.6 mm<sup>2</sup>, highlighted by a pink rectangle in Fig. 5.1 (frame 54204).  
 421 This region corresponds to the one where the correlation with the probe LPA47 depicts a maximum as presented  
 422 in the top image of Fig. 4.4. Note that positive velocities  $v_r$  and  $v_\theta$  mean outwards and downwards, respectively.

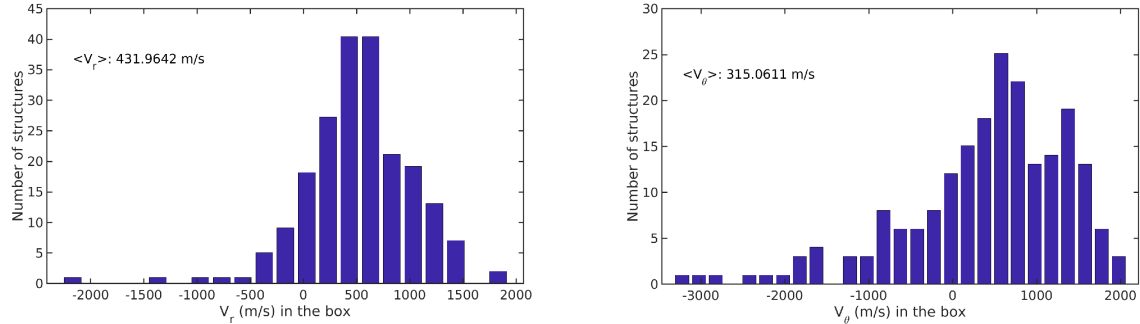


Figure 5.2: Perpendicular and tangential velocity distributions (left and right, respectively) calculated with TRACK in the small region delimited by the pink rectangle in figure 5.1. The step of the distribution is 200 m/s. The average radial and poloidal velocities are also indicated on the picture.

423 As can be seen in Fig. 5.2, the distributions are quite wide with  $v_r$  ranging from -500 to 1500 m/s and  $v_\theta$  from  
 424 -2000 to 2000 m/s, values coherent to what can usually be observed on COMPASS [13, 22]. It is interesting to  
 425 note that most structures are statistically experiencing a movement outwards and downwards but that some of  
 426 them move in the opposite direction, mostly upwards but some of them also inwards, with non-negligible velocities.  
 427 This behavior is not surprising in a turbulent media and was reported in many edge turbulence codes (see Ref. [12]  
 428 for instance), but can only be investigated by individually tracking single structures movements. It appears that  
 429 the blob depicted in Fig. 5.1 is amongst the 25% fastest structures in the perpendicular direction and the fastest  
 430 structure in the tangential direction. Despite its qualitative behaviour seems representative of many other observed  
 431 structures, it is certainly not the case from a quantitative point of view. In addition, the existence of counter-  
 432 propagating structures at the same location demonstrates that the turbulence dynamics is actually more complex  
 433 than what a short sequence suggests. Last but not least, it is important to point out that cross-correlation techniques  
 434 usually applied to gas-puff imaging data [10] would show the main motion outwards and downwards with an average  
 435 velocity of order of few hundreds meters per second, hiding the real structure motion.

## 436 6 Conclusions and perspectives

437 The tomographic reconstruction technique presented in Ref. [31] for circular plasmas was successfully applied to  
 438 camera data recorded at a frame rate of 270 kfps during a D-shaped plasma discharge of COMPASS. The robustness  
 439 of the method was tested using slowly varying emissivity signals along the field lines (up to 20% on the total field  
 440 of view of the camera) coming from a TOKAM3X simulation [28]. Even in that case, the tomographic inversion  
 441 shows that the main poloidal features can be well retrieved. Then, the inversion of real camera data was compared  
 442 to the ion saturation currents measured by different probes in the divertor of the COMPASS tokamak. Probes  
 443 that are magnetically connected to the reconstructed poloidal plane from the camera data show a high (up to 0.4)  
 444 normalized correlation, at a location in the poloidal plane close to the one magnetically connected to the probe,  
 445 showing that the camera signal records similar edge plasma structures as the ion saturation current. On the other  
 446 hand, probes that are not magnetically connected to the plane show a very low correlation. The method is further  
 447 validated by looking at the time delay obtained from the maximum of correlation at the position of the poloidal  
 448 plane magnetically connected to the divertor probes. Its values stay constant for different probes, even though  
 449 the position magnetically linked to the probe in the poloidal plane changes and the distance along the field line  
 450 stays constant. This confirms that the reconstruction method correctly redistributes the camera signal at the right  
 451 location on the poloidal plane. The reconstructed data can then be used with confidence and allow to study edge  
 452 tokamak physics with some advantages compared to what other diagnostics can offer, such as gas-puff imaging or  
 453 probes.

454 For instance, unlike gas-puff imaging [33] or probes [30, 8, 7], the light observation coming from the interaction  
 455 of the neutral gas naturally present in the SOL is completely passive and non-perturbative. In addition, the spatial  
 456 resolution in the radial and poloidal directions can be much higher than what probes can provide. Moreover, this  
 457 technique does not bound the observation in one given poloidal plane but any poloidal plane within the field of view  
 458 of the camera can be reconstructed. Last, as shown in this article, the camera observes turbulent structures located  
 459 near the separatrix, location where probes cannot measure for a long time without globally perturbing the plasma  
 460 and being eroded. On the other hand, the method also has some disadvantages that one has to consider. The whole

461 inversion method, letting apart for the code development, requires high computational resources, especially if the  
462 magnetic field is varying. In addition, as for GPI, no clear model exists to link the plasma edge emissivity to any  
463 physical quantity without knowing the electron density and temperature profiles, gas influx, impurity contents etc...  
464 Furthermore, uncertainties in the reconstruction method linked to the difficult spatial calibration of the camera and  
465 uncertainties in the magnetic field reconstruction can modify the dynamic of blobs in the reconstructed poloidal  
466 plane. In addition, even though improving fast, nowadays cameras are still on the technological edge to study fast  
467 movement that can happen at the shear flow location, as we have shown in Section 5. Last, the signal is localized  
468 only in a region where the interaction from the neutral gas and the plasma is strongest, limiting the region of  
469 interest. However, this region is localized near the separatrix which is a region of major interest.

470 An other problem to tackle is the automatic analysis of reconstructed video that often represents several gigabytes  
471 of data. Within this enormous amount of data, one has to automatically detect the turbulent structures and then  
472 track them. The contour of these structures is rather well defined, as one can see in Fig. 4.3 for instance, allowing to  
473 detect them easily. On the other hand, following the structure is more challenging as they change in shape, directions  
474 and intensity on frame to frame basis, especially near the shear flow region. The high acquisition speed of the camera  
475 helps to reduce this difficulty but improvement shall arise with new generations of fast and highly sensitive cameras.  
476 Nevertheless, it was shown that using the TRACK software [5], it is possible to efficiently analyze complete videos  
477 with fully automatic processing techniques. The automatic extraction of the main structures characteristics, such as  
478 their velocity, size, aspect ratio, and orientation, in a variety of discharge conditions offers many perspectives for a  
479 better understanding of turbulence in the vicinity of the separatrix. It can, for instance, provide statistically reliable  
480 experimental data enabling a more straightforward comparison with simulation results or theoretical models. In  
481 addition, comparison with other diagnostics can be performed and provide valuable insight. Last, MHD modes or  
482 instabilities influencing the blobs dynamic can also be investigated as instabilities can also be detected by visible  
483 light observations [17].

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